PHY 752 – Problem Set #8

Read Chapter 8 & 2 in Marder

1. Consider a one-dimensional tight-binding model system described by a tridiagonal Hamiltonian which has non-trivial matrix elements $H_{nn'}$ of the form:

$$H_{nn} = \alpha$$
 and $H_{n(n\pm 1)} = \beta$

for all site indices n, where α and β are real energy parameters.

- (a) Consider the case where the site indices n, n' take the values 1, 2, 3 exclusively and find the eigenvalues.
- (b) Consider the case where the site indices n, n' take the values $1 \dots 8$ exclusively and find the eigenvalues.
- (c) Consider the case where the site indices n, n' have an infinite range $(-\infty \le n, n' \le \infty)$. Compare the energy range for this system with that of the previous two samples.