

First principles modeling of electrolyte/anode interfaces in an all-solid state battery –



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Outline

- **Motivation**
 - **Why all solid state batteries**
 - **Why γ -Li₃PS₄/Li**
- **Computational methods**
- **Results**
 - γ -Li₃PS₄/Li
 - **Other interfaces -- β -Li₃PO₄/Li, *SD*-Li₂PO₂N**
 - γ -Li₃PS₄/LiS₂/Li
- **Summary and conclusions**

Motivation – why all solid state batteries ?

- **Advantages in stability, efficiency, and safety**
- **Promising new materials with increased conductivity**

Anomalous High Ionic Conductivity of Nanoporous $\beta\text{-Li}_3\text{PS}_4$

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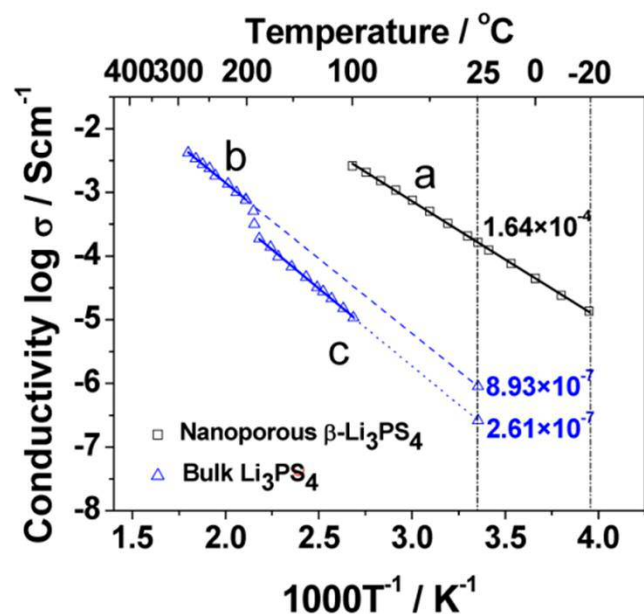


Figure 1. Arrhenius plots for nanoporous $\beta\text{-Li}_3\text{PS}_4$ (line a), bulk $\beta\text{-Li}_3\text{PS}_4$ (line b), and bulk $\gamma\text{-Li}_3\text{PS}_4$ (line c). The conductivity data for bulk Li_3PS_4 are reproduced from the work of Tachez.¹⁰

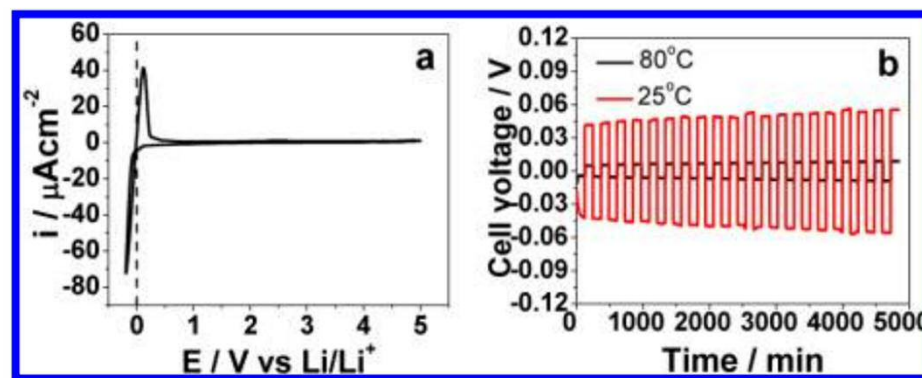


Figure 5. Electrochemical stability of $\beta\text{-Li}_3\text{PS}_4$ and cycling stability with metallic lithium electrodes. (a) CV of a $\text{Li}/\beta\text{-Li}_3\text{PS}_4/\text{Pt}$ cell, where Li and Pt serve as the reference/counter and working electrodes, respectively. (b) Lithium cyclability in a symmetric $\text{Li}/\beta\text{-Li}_3\text{PS}_4/\text{Li}$ cell. The cell was cycled at a current density of 0.1 mA cm^{-2} at room temperature and $80 \text{ }^\circ\text{C}$.

Summary of “first-principles” calculation methods

Exact problem :

$$\mathcal{H}(\{\mathbf{r}_i\}, \{\mathbf{R}^a\}) \Psi_\alpha(\{\mathbf{r}_i\}, \{\mathbf{R}^a\}) = E_\alpha \Psi_\alpha(\{\mathbf{r}_i\}, \{\mathbf{R}^a\})$$

Electronic coordinates

Atomic coordinates

Born-Oppenheimer approximation

Born & Huang, **Dynamical Theory of Crystal Lattices**,
Oxford (1954)

Density functional theory

Hohenberg and Kohn, *Phys. Rev.* **136** B864 (1964)

Kohn and Sham, *Phys. Rev.* **140** A1133 (1965)

Approximately equivalent problem :

Ground state energy (mean field approximation) : $E_0(\mathbf{r}, \rho(\mathbf{r}), \{\mathbf{R}^a\})$

Electron
density

$$H_{eff}(\mathbf{r}, \rho(\mathbf{r}), \{\mathbf{R}^a\}) \psi_n(\mathbf{r}) = \varepsilon_n \psi_n(\mathbf{r})$$

$$\rho(\mathbf{r}) = \sum |\psi_n(\mathbf{r})|^2 \quad H_{eff}(\mathbf{r}, \rho(\mathbf{r}), \{\mathbf{R}^a\}) = \frac{\delta E_0(\mathbf{r}, \rho(\mathbf{r}), \{\mathbf{R}^a\})}{\delta \rho(\mathbf{r})}$$

More computational details:

$$H_{eff}(\mathbf{r}, \rho(\mathbf{r}), \{\mathbf{R}^a\}) = -\frac{\hbar^2 \nabla^2}{2m} + \sum_a \underbrace{\frac{-Z^a e^2}{|\mathbf{r} - \mathbf{R}^a|}}_{\text{electron-nucleus}} + e^2 \int d^3 r' \underbrace{\frac{\rho(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|}}_{\text{electron-electron}} + \underbrace{V_{xc}(\rho(\mathbf{r}))}_{\text{exchange-correlation}}$$

Exchange-correlation functionals:

LDA: J. Perdew and Y. Wang, Phys. Rev. B **45**, 13244 (1992)

GGA: J. Perdew, K. Burke, and M. Ernzerhof, PRL **77**, 3865 (1996)

HSE06: J. Heyd, G. E. Scuseria, and M. Ernzerhof, JCP **118**, 8207 (2003)

Numerical methods:

“Muffin-tin” construction: Augmented Plane Wave developed by Slater → “linearized” version by Andersen:

J. C. Slater, Phys. Rev. **51** 846 (1937)

O. K. Andersen, Phys. Rev. B **12** 3060 (1975) (LAPW)

Pseudopotential methods:

J. C. Phillips and L. Kleinman, Phys. Rev. **116** 287 (1959) -- original idea

P. Blöchl, Phys. Rev. B. **50** 17953 (1994) – Projector Augmented Wave (PAW) method

Outputs of calculations:

Ground state energy :

$E_0(\mathbf{r}, \rho(\mathbf{r}), \{\mathbf{R}^a\}) \Rightarrow$ Determine formation energies

$\min_{\{\mathbf{R}^a\}} (E_0(\mathbf{r}, \rho(\mathbf{r}), \{\mathbf{R}^a\})) \Rightarrow$ Determine structural parameters

\Rightarrow Stable and meta - stable structures

\Rightarrow Normal modes of vibration

$\rho(\mathbf{r}) = \sum_n |\psi_n(\mathbf{r})|^2 \Rightarrow$ Self - consistent electron density

$\{\varepsilon_n\} \Rightarrow$ One - electron energies; densities of states

Codes: ATOMPAW \rightarrow PAW atomic data files (<http://pwpaw.wfu.edu>)

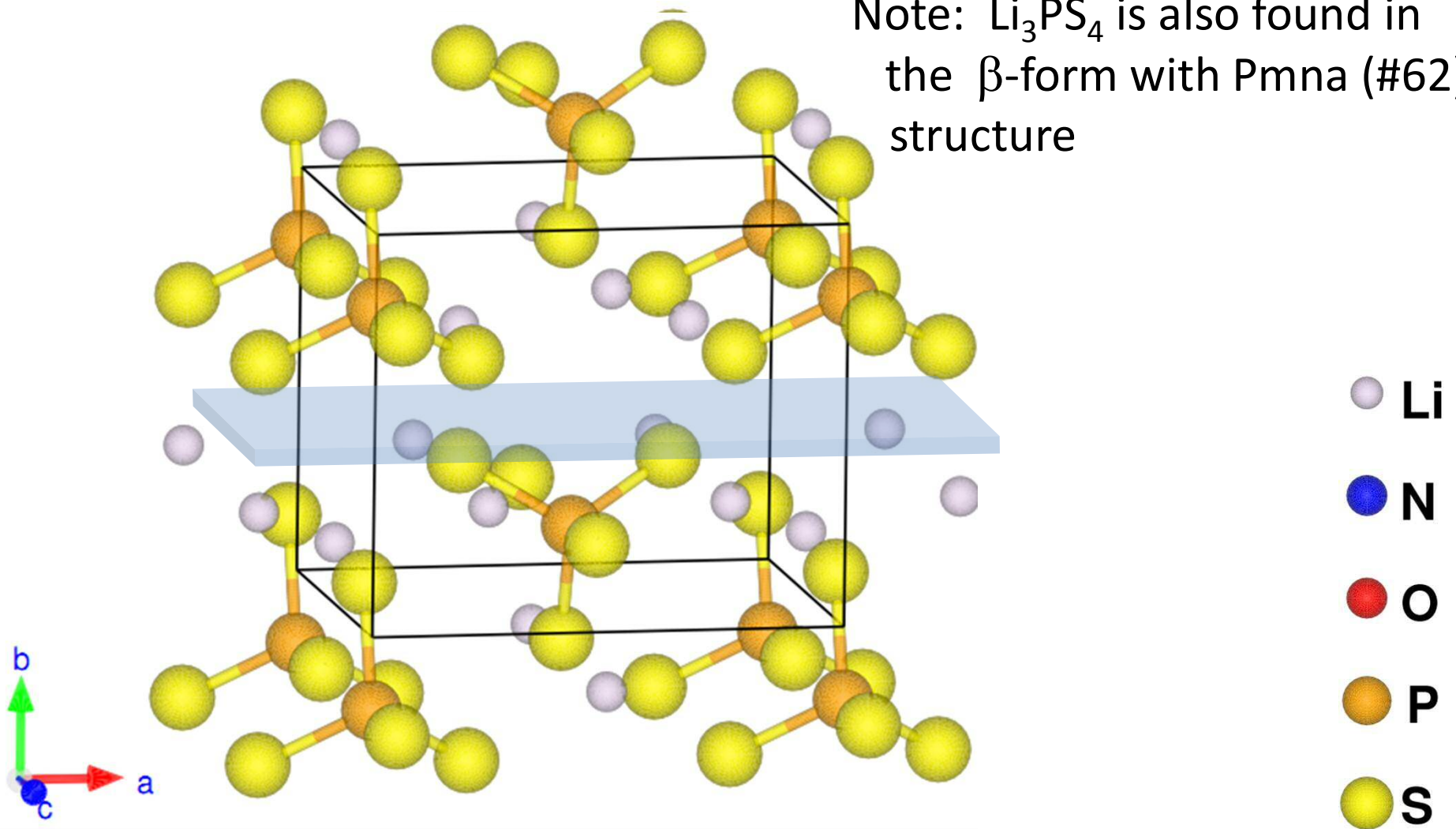
ABINIT \rightarrow DFT for materials (<http://www.abinit.org>)

PWSCF \rightarrow DFT for materials (<http://quantum-espresso.org>)

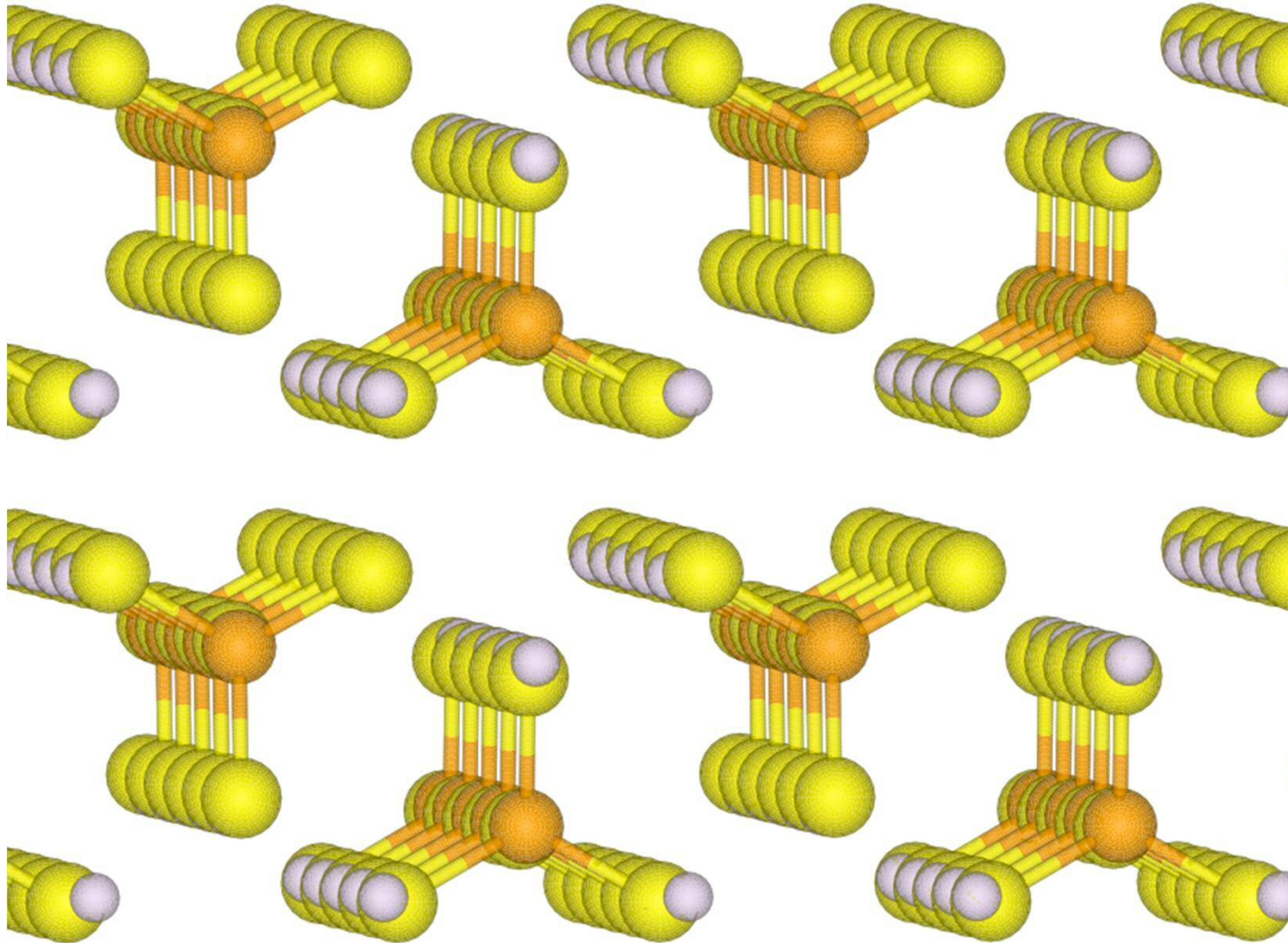
VESTA \rightarrow visualization (<http://jp-minerals.org/vesta/en>)

Crystal structure of bulk Li_3PS_4 – γ -form $\text{Pmn}2_1$ (#31)

Note: Li_3PS_4 is also found in the β -form with Pmna (#62) structure

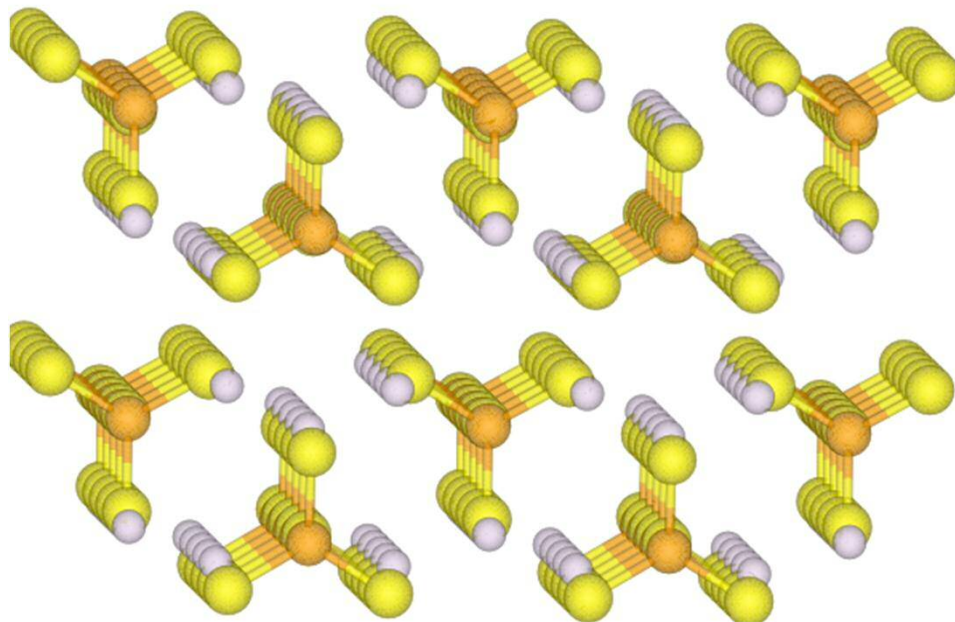


γ -Li₃PS₄ [0 1 0] surface

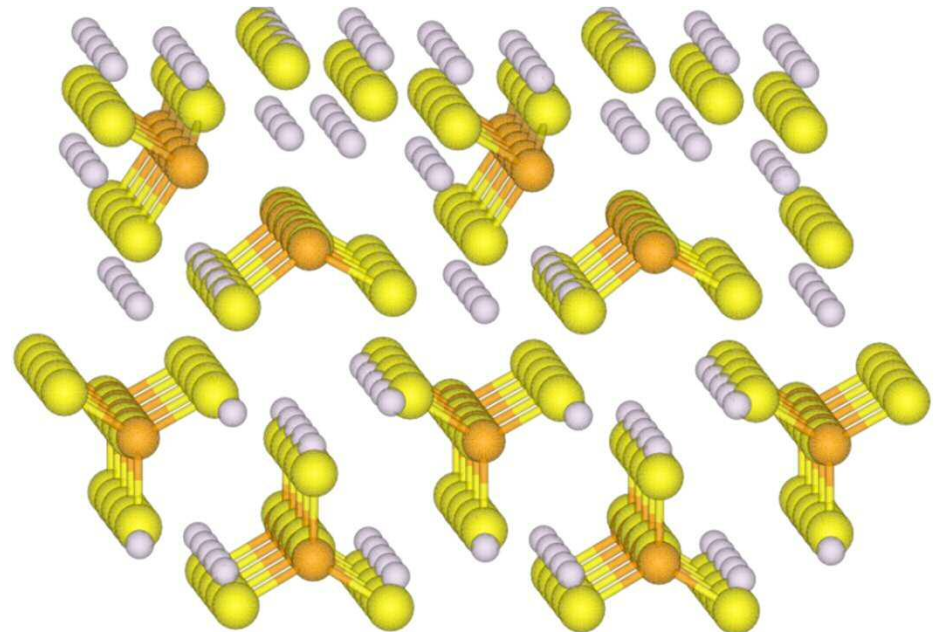


Simulations of ideal γ -Li₃PS₄ [0 1 0] surface in the presence of Li

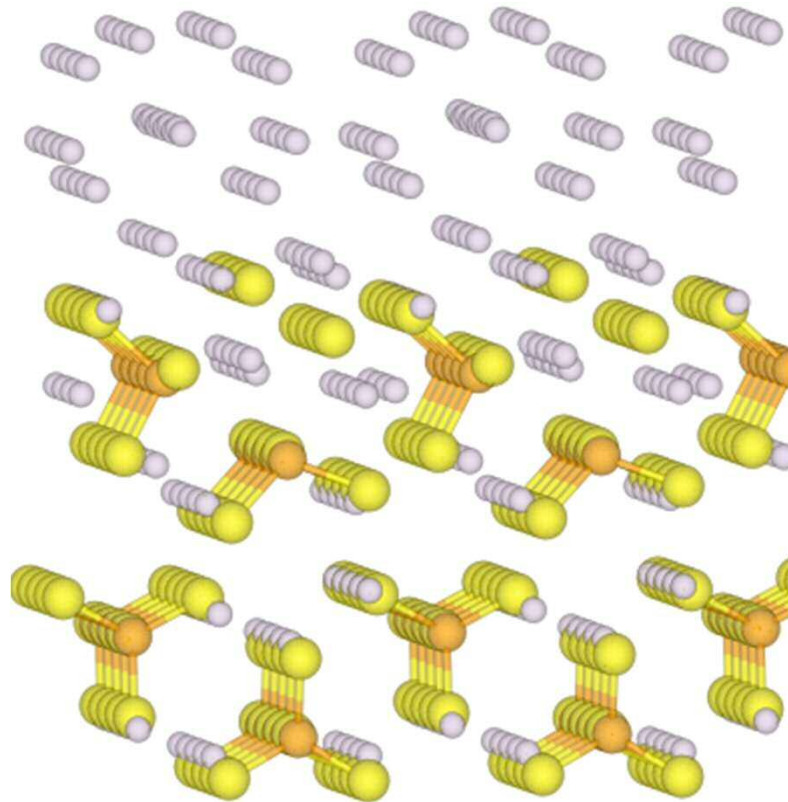
Initial configuration:



Computed optimized
structure:

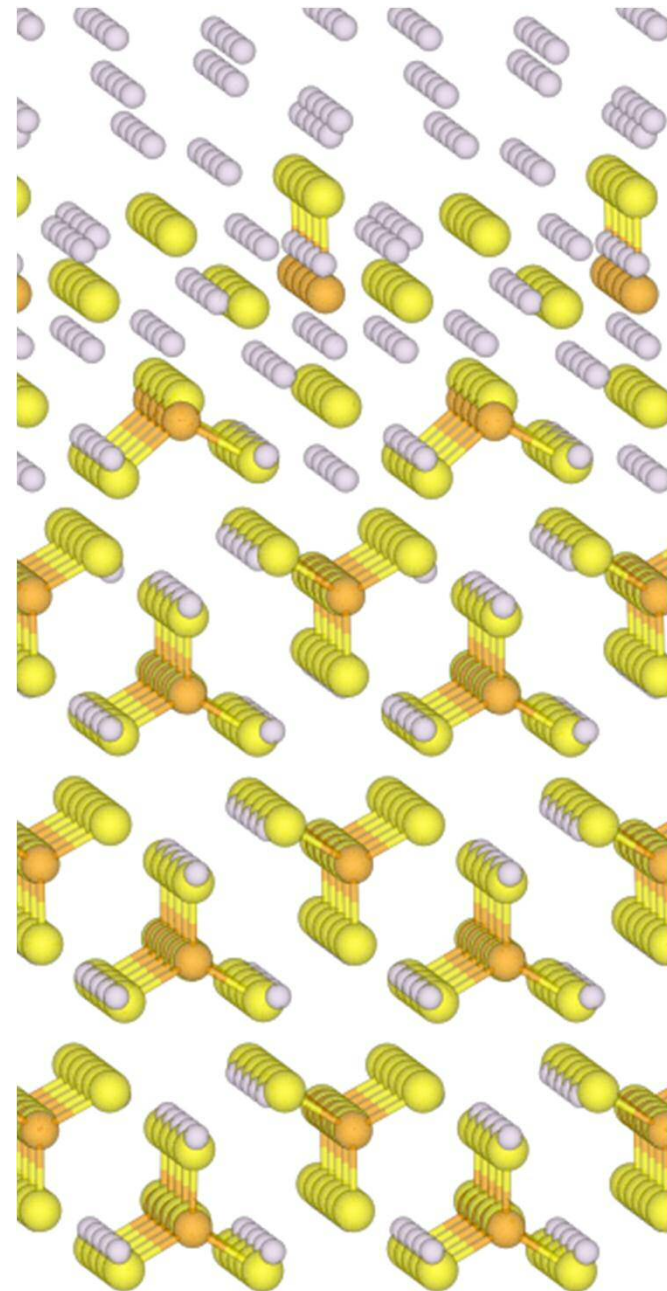


**More simulations of ideal
 γ -Li₃PS₄ [0 1 0] surface
in the presence of Li –
supercells containing
12 Li atoms and
2 or 4 electrolyte layers**



10/29/2013

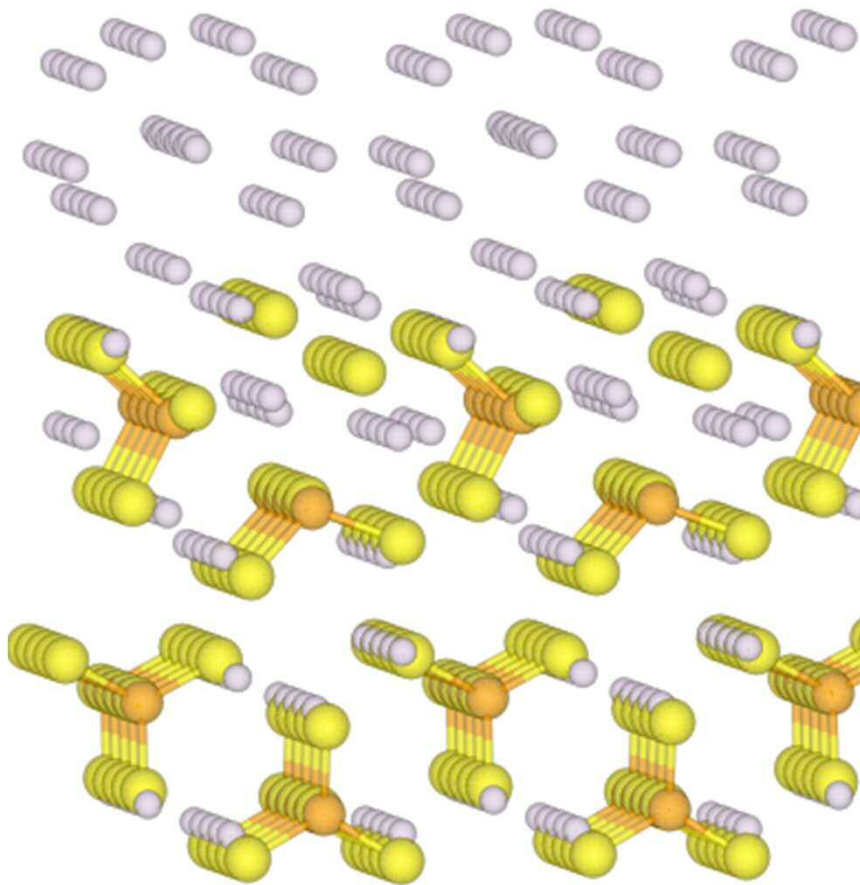
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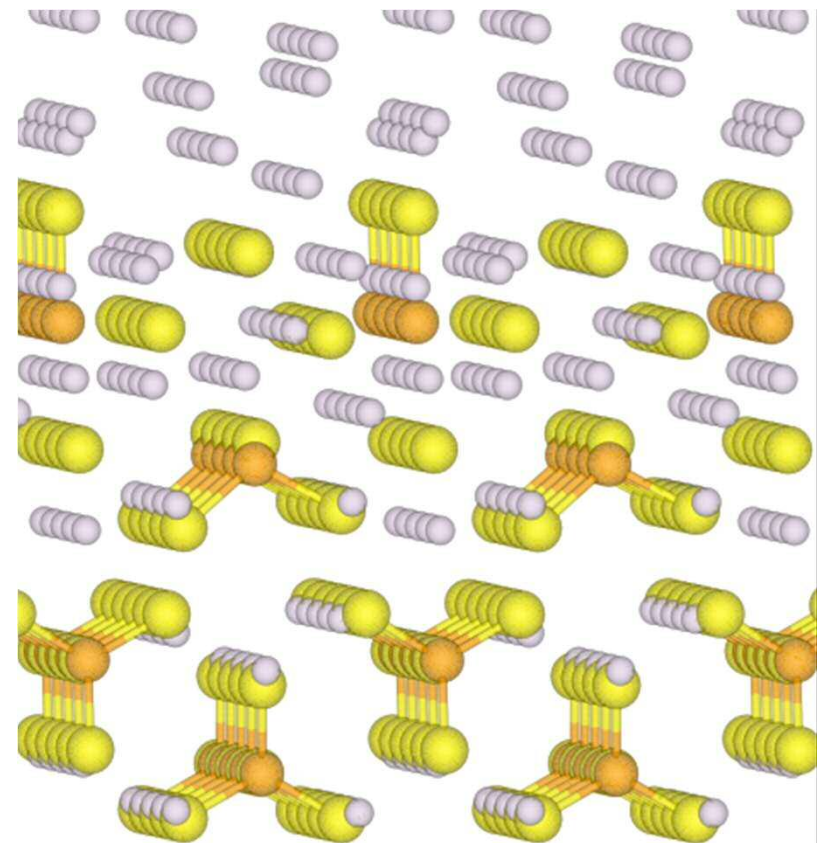
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γ -Li₃PS₄ [0 1 0] surface in the presence of Li –
supercells containing 12 Li atoms and 2 or 4 electrolyte layers
(greater detail)

2 electrolyte layers



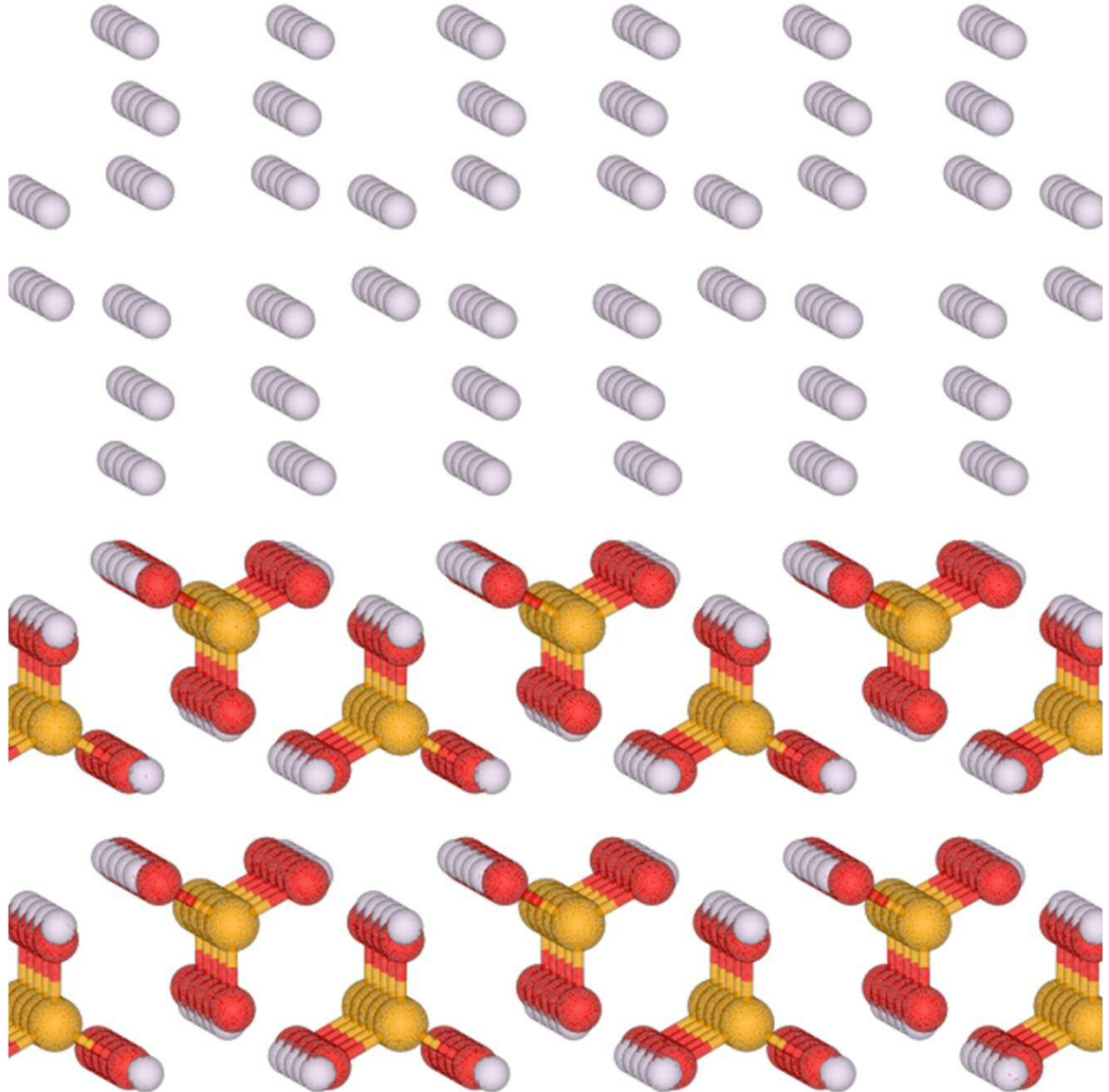
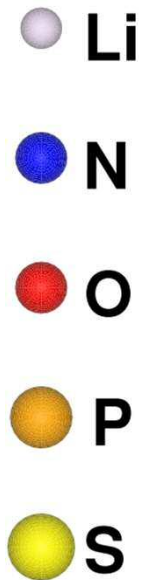
4 electrolyte layers



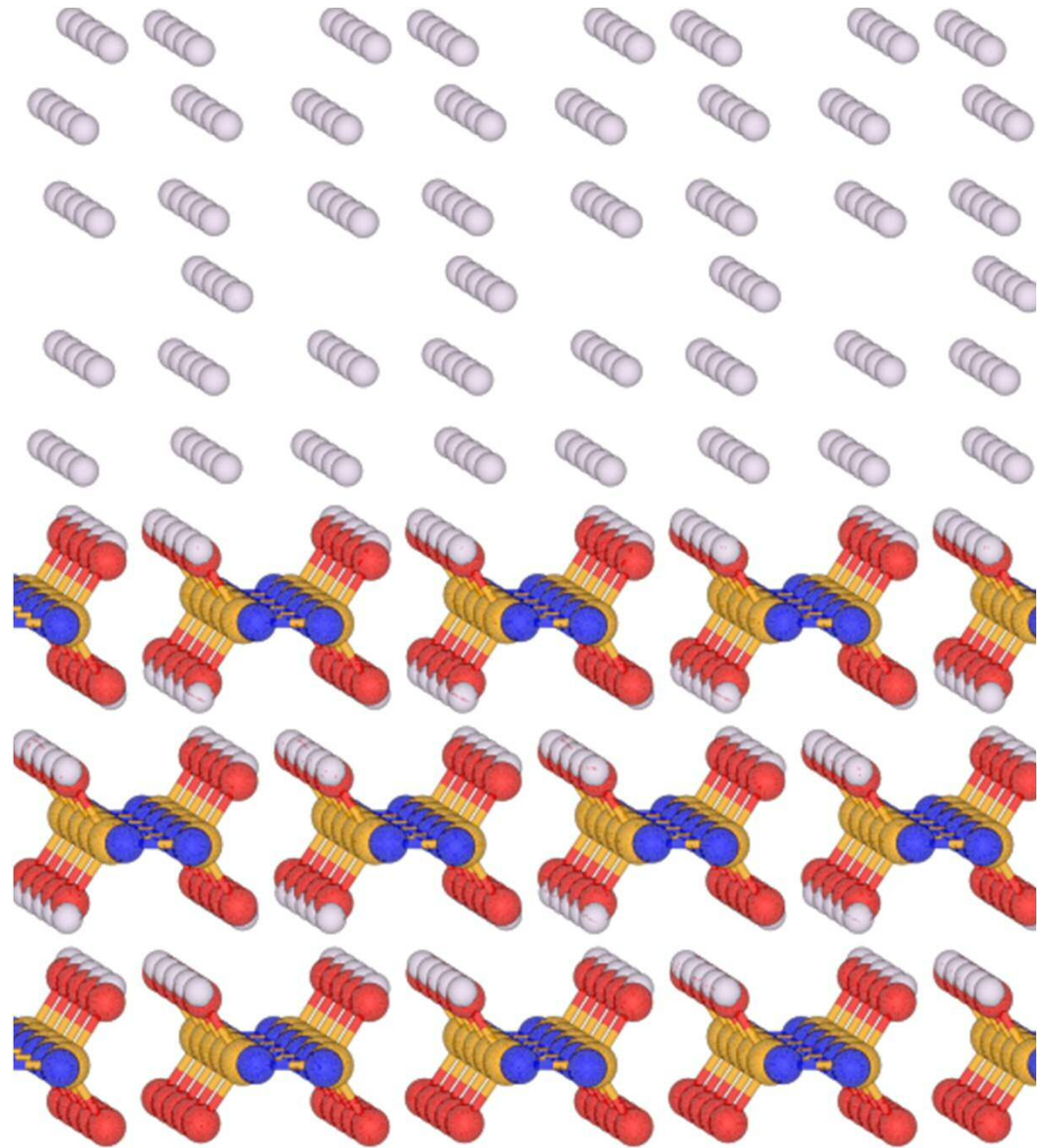
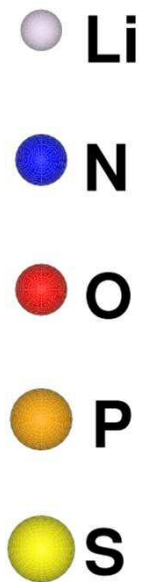
Mystery:

- **Models of ideal Li_3PS_4 surfaces are computational found to be structurally (and chemically) altered by the presence of Li metal. (Also found for $\beta\text{-Li}_3\text{PS}_4$ and for various initial configurations of Li metal.)**
- **Experimentally, the ORNL group has found that solid Li_3PS_4 electrolyte samples can be prepared in Li/ Li_3PS_4 /Li cells and cycled many times**

Computational counter example – stable interface: $\text{Li}/\beta\text{-Li}_3\text{PO}_4$



Computational counter example – stable interface: $\text{Li}/\text{SD-Li}_2\text{PO}_2\text{N}$



Back to mystery:

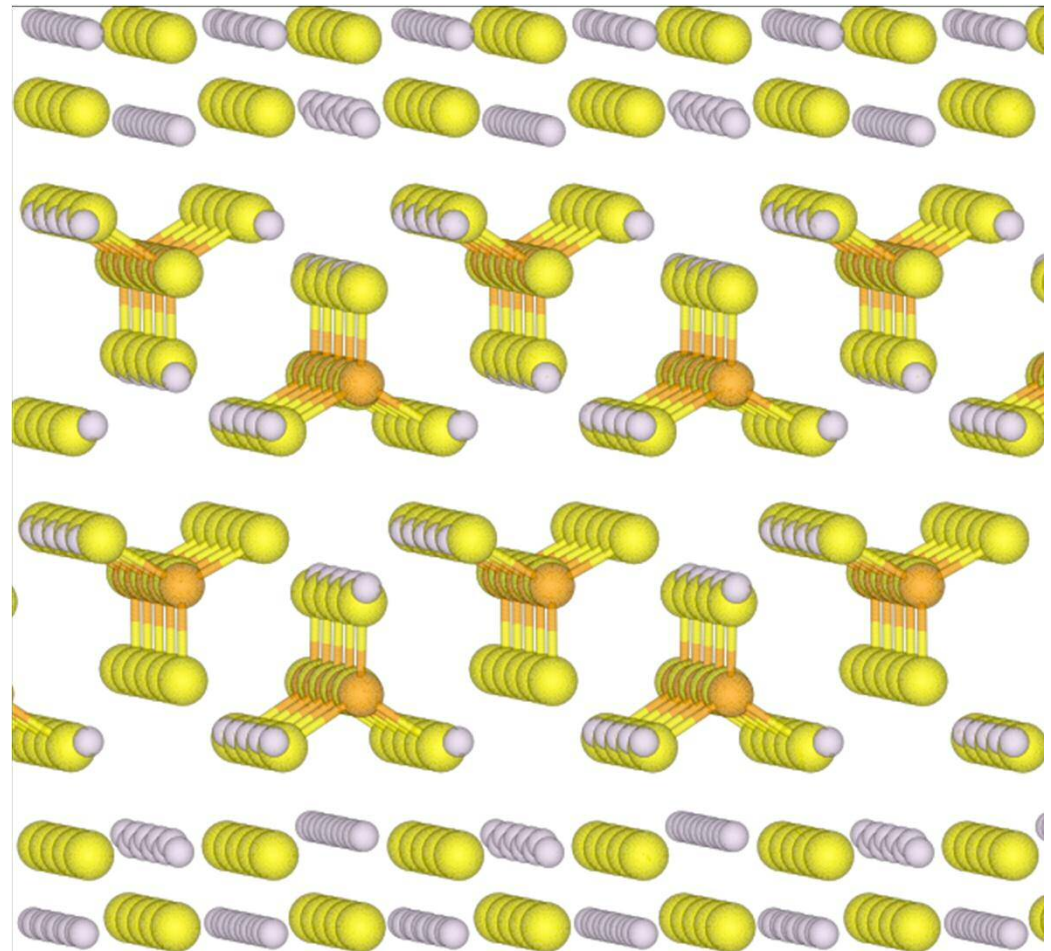
- **Models of ideal Li_3PS_4 surfaces are computational found to be structurally (and chemically) altered by the presence of Li metal. (Also found for $\beta\text{-Li}_3\text{PS}_4$ and for various initial configurations of Li metal.)**
- **Experimentally, the ORNL group has found that solid Li_3PS_4 electrolyte samples can be prepared in Li/ Li_3PS_4 /Li cells and cycled many times.**

Possible solution:

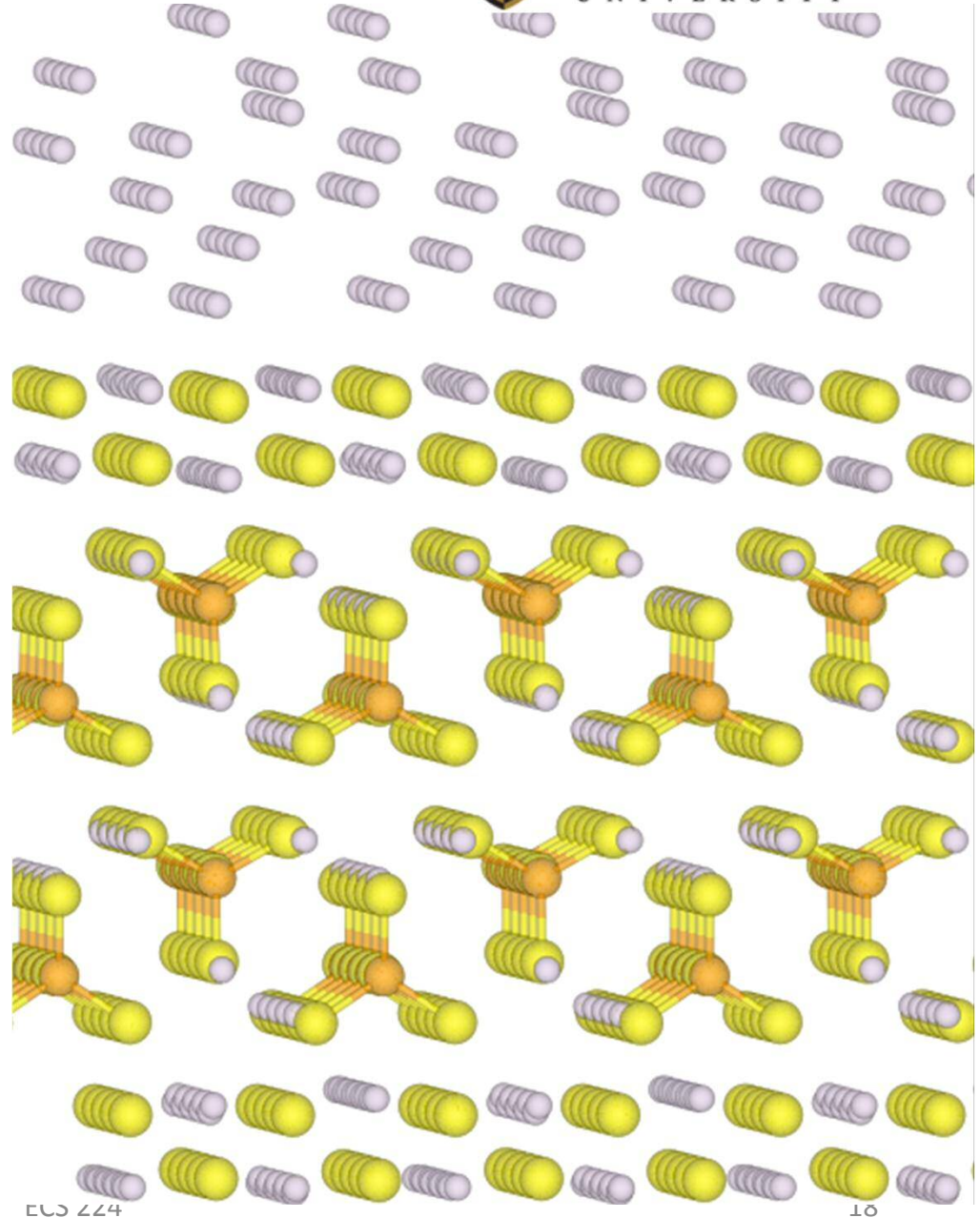
- **Thin protective buffer layer at Li_3PS_4 surface can stabilize electrolyte – for example $\text{Li}_2\text{S}/\text{Li}_3\text{PS}_4/\text{Li}_2\text{S}$**

Idealized $\text{Li}_2\text{S}/\text{Li}_3\text{PS}_4/\text{Li}_2\text{S}$ system

Details:
Thin film of cubic Li_2S oriented in its non-polar $[1\ 1\ 0]$ direction, optimized on $[0\ 1\ 0]$ surface of $\gamma\text{-Li}_3\text{PS}_4$. While the Li_2S film was slightly strained, the binding energy of the composite was found to be stable with a binding energy of $-0.9\ \text{eV}$.



**Idealized $\text{Li}_2\text{S}/\text{Li}_3\text{PS}_4/\text{Li}_2\text{S}$
system optimized
in presence of Li**



Summary and conclusions:

- Models of ideal Li_3PO_4 and $\text{Li}_2\text{PO}_2\text{N}$ surfaces are computational found to be structurally stable in the presence of Li metal.
- Models of ideal Li_3PS_4 surfaces are computational found to be structurally (and chemically) altered by the presence of Li metal. (Also found for $\beta\text{-Li}_3\text{PS}_4$ and for various initial configurations of Li metal.)
- Thin protective buffer layer of Li_2S at Li_3PS_4 surface can stabilize electrolyte; $\text{Li}_2\text{S}/\text{Li}_3\text{PS}_4/\text{Li}_2\text{S}$ is found to be stable in the presence of Li metal.
- Experimentally, the ORNL samples of solid Li_3PS_4 electrolyte, prepared in $\text{Li}/\text{Li}_3\text{PS}_4/\text{Li}$ cells and cycled many times, may form thin buffer layer in first few cycles.