

Name \_\_\_\_\_  
Final Exam  
December 9, 2005

This test consists of five parts. Please note that in parts II through V, you can skip one question of those offered.

**Part I: Multiple Choice (mixed new and review questions) [50 points]**

For each question, choose the best answer (2 points each)

1. The following masses are listed in the book as masses of some of the isotopes of Mg. Which one is clearly a misprint?  
A) 22.994124 u  
B) 23.985042 u  
C) 26.985838 u  
D) 27.984341 u  
E) 28.375346 u
  
2. When calculations were done for the amount of energy density in a thermal background of electromagnetic energy, the result, before quantum theory was developed, was  
A) Zero  
B) A non-zero amount, but less than the experimental value  
C) Exactly the right amount, but at the wrong wavelengths  
D) A finite amount, but more than the experimental values  
E) Infinity
  
3. Which of the following is *not* consistent with special relativity?  
A) Time is the fourth dimension  
B) It is always possible to tell which of two objects is actually moving based on how fast their clocks are running compared to each other  
C) Which of two events occurred first may be disagreed on by different observers  
D) There are no truly rigid objects in special relativity  
E) Objects moving at high speed appear to be shorter, as viewed by stationary observers

4. According to the Bohr model (and current quantum mechanics), the reason that only certain wavelengths come out of atoms like hydrogen is because
- A) The electrons can only exist at certain energy levels; the differences in energy determine the wavelengths of light that come out
  - B) The atoms have a particular size, and only certain wavelengths of light will fit inside those atoms
  - C) The multiple electrons in the atoms are spaced at precisely those wavelengths, and they radiate together to make the wave
  - D) The electrons orbit at exactly the corresponding frequencies, so that's the frequencies that come out
  - E) The electrons themselves have that wavelength, and coherently generate only those wavelengths
5. One observation that helped lead Einstein to the general theory of relativity was that
- A) Heavy objects fall slightly faster than light objects
  - B) Objects in gravitational fields move in curved lines; other forces cause them to move in straight lines
  - C) Gravity always causes the velocity of objects to be downwards
  - D) Objects should be able to produce gravity waves, but in Newton's theory, they cannot
  - E) The effects of gravity are indistinguishable from the effects of being in an accelerated reference frame
6. In  $\beta^+$ -decay, what particle comes out of a nucleus, besides a neutrino?
- A) A  ${}^4\text{He}$  nucleus
  - B) An electron
  - C) A proton
  - D) An anti-electron, also called a positron
  - E) A neutron
7. If I tell you are looking at a 5p electron, I mean that
- A)  $n = 5$  and  $l = 3$
  - B)  $n = 3$  and  $l = 5$
  - C)  $n = 5$  and  $l = 1$
  - D)  $n = 1$  and  $l = 5$
  - E)  $n = 5$  and  $l = 5$
8. When you get near a massive object, according to general relativity,
- A) Time runs at a constant rate, even if you are moving
  - B) Time depends on the mass, not just the speed, of the observer
  - C) Time speeds up
  - D) Time slows down
  - E) Time runs in reverse
9. If two objects are moving towards each other, each moving at  $2/3$  the speed of light, then as viewed by one of them, the other one will be moving

- A) Faster than the speed of light (definitely)
  - B) Slower than the speed of light (definitely)
  - C) At the speed of light (definitely)
  - D) Either faster or slower, depending on which person is actually moving
  - E) There is insufficient information to answer this question
10. If  $q$  stands for a quark, and  $\bar{q}$  stands for an anti-quark, which combination does not seem to occur in nature?
- A)  $qqq$     B)  $\bar{q}\bar{q}\bar{q}$     C)  $\bar{q}q$     D)  $\bar{q}qq$     E) Actually, these all do occur in nature
11. What is the stress-energy tensor  $T_{\mu\nu}$  that is described in general relativity?
- A) It represents the gravitational force on some object
  - B) It contains the energy density, momentum density, and other quantities that cause spacetime curvature
  - C) It contains the energy density, but none of the other quantities, that cause spacetime curvature
  - D) It describes the curvature of spacetime
  - E) It describes the distance formula in curved spacetime
12. Momentum has three components, but in four dimensions, it becomes a four-dimensional vector whose fourth component is closely related to
- A) time    B) velocity    C) mass    D) angular momentum    E) energy
13. Which of the following is not a condition that the wave function  $\psi(x,t)$  must satisfy, in general?
- A) It must be continuous
  - B) It must be finite
  - C) It must have a continuous derivative, if the potential energy is finite
  - D) It must fall off to zero at infinity
  - E) It must be real
14. What is the name of the isotope that contains 18 neutrons and 17 protons?
- A)  $^{18}\text{Cl}$     B)  $^{17}\text{Cl}$     C)  $^{35}\text{Cl}$     D)  $^{17}\text{Ar}$     E)  $^{35}\text{Ar}$
15. The basic reason that heavy nuclei (like Uranium) have more neutrons than protons is because
- A) The positively charged protons don't like to be near each other; neutrons don't mind being near each other
  - B) The strong force is slightly stronger between neutrons than it is between protons
  - C) The neutron is a little heavier than the proton
  - D) There are so many electrons around that a few protons are bound to capture some and become neutrons
  - E) Protons must obey the Pauli exclusion principle; neutrons need not
16. DeBroglie found there was a direct relationship between the wavelength of a wave and the \_\_\_\_\_ of a particle

A) energy    B) mass    C) frequency    D) momentum    E) velocity

17. What is the meaning of the *group velocity* of a wave?
- A) It is how fast an individual peak of a wave moves
  - B) It is how fast an individual trough of a wave moves
  - C) It is how fast the wave, as a whole, moves
  - D) It is how fast the frequency changes
  - E) It is how fast the wavelength changes
18. There are a pair of neutron stars that are orbiting each other. Observations indicate that the two stars are slowly moving closer together. The reason is that
- A) Friction caused by rubbing against the bumpy metric (distance formula) causes them to slow down and gradually spiral towards each other
  - B) Orbits in general relativity are not ellipses, but rather spirals that very slowly bring the two objects together
  - C) Gravity waves are emitted by the pair of neutron stars, draining energy from the system
  - D) Gravitational flux tubes connecting the pair gradually pull them together
  - E) The moving together is an illusion caused by the relativistic velocities, making the distance seem to shrink due to Lorentz contraction

***In questions 19-21, you will answer questions about a particle made of an up quark and strange anti-quark,  $[u\bar{s}]$***

19. What type of particle is made of  $[u\bar{s}]$ ?
- A) lepton    B) anti-lepton    C) meson    D) baryon    E) anti-baryon
20. The charge of the particle made from  $[u\bar{s}]$  is
- A) -1    B) -1/3    C) 0    D) +1/3    E) +1
21. The strangeness of the particle  $[u\bar{s}]$  is
- A) -2    B) -1    C) 0    D) +1    E) +2

In questions 22 – 25, you will be given a reaction, and you must state what type of interaction it is. A mini-table of particles is listed at right. All of them have spin  $\frac{1}{2}$  and strangeness 0.

22.  $\mu^+ + \mu^- \rightarrow \text{photon} + \text{photon}$  (the  $\mu^+$  is the anti-particle of the  $\mu^-$ )  
 A) impossible B) strong C) weak D) electromagnetic E) gravity
23.  $n^0 + \nu_\mu \rightarrow p^+ + \mu^-$   
 A) impossible B) strong C) weak D) electromagnetic E) gravity
24.  $n^0 + \bar{n}^0 \rightarrow p^+ + \bar{p}^-$  (the  $\bar{n}^0$  and  $\bar{p}^-$  are the anti-particles of the  $n^0$  and  $p^+$ )  
 A) impossible B) strong C) weak D) electromagnetic E) gravity
25.  $\mu^- + \mu^- \rightarrow \text{photon} + \text{photon}$   
 A) impossible B) strong C) weak D) electromagnetic E) gravity

Baryons	
Name	Mass
$p^+$	938
$n^0$	940
Leptons	
Name	Mass
$\mu^-$	106
$\nu_\mu$	0
Other	
Name	Mass
photon	0

**Part II: Short answer (review material) [20 points]**

Choose **two** of the following three questions and give a short answer (1-3 sentences) (10 points each).

26. In the twin paradox, one twin stays on Earth while the other travels around in space, eventually returning to Earth. Which one is younger, if either, and explain how it makes sense to know which one is “really” moving.
27. Explain, using the uncertainty principle, why an electron in an atom doesn’t just go to the nucleus at the origin, but instead is spread out.
28. A hydrogen atom is described by four quantum numbers: the energy value  $n$ , the total angular momentum  $l$ , the  $z$ -component of the angular momentum  $m$ , and the  $z$ -component of the spin  $m_s$ . Suppose these take the values  $-2$ ,  $+\frac{1}{2}$ ,  $2$ , and  $4$ , not respectively. Which one is which, *i.e.*, which of these is  $n$ ,  $l$ ,  $m$ , and  $m_s$ ?

**Part III: Short answer (new material) [30 points]**

Choose **three** of the following four questions and give a short answer (1-3 sentences) (10 points each).

29. There is an atom whose electrons take the configuration

$$1s^2 2s^2 2p^6 3s^2 3p^6 4s^1 3d^5$$

What type of atom is this? According to the rules we talked about in class, what *should* the electronic configuration be?

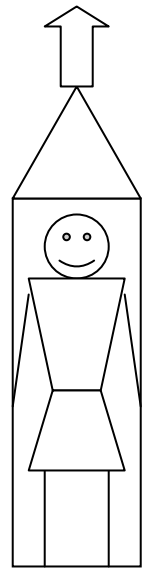
30. Explain, qualitatively, why most stable nuclei have approximately equal numbers of protons and neutrons.
31. What are the names of the six quarks in the standard model of particle physics? Give the electric charges of at least two of them.

32. Explain how the orbit of a planet like Mercury differs, according to general relativity, from the predictions of Newton's theory of gravity.

**Part IV: Calculation (review material) [40 points]**

Choose **two** of the following three questions and perform the indicated calculations (20 points each)

33. A woman who has just become pregnant has a mass of 69.0 kg. She gets aboard a spacecraft traveling at a velocity of  $2.9 \times 10^8$  m/s.
- What is her total energy  $E$ , as measured by us?
  - Assuming her baby takes the usual 0.75 years to gestate, as measured by her, how long will it be until the baby is born, according to us?
  - How far will she have traveled in this amount of time? 1 year =  $3.15 \times 10^7$  s.
  - The woman is 169 cm tall and measures 92 cm around her hips. What are the same two measurements, according to observers on the Earth? The rocket is traveling in the direction of her height.



34. A photon with wavelength 297 nm strikes a metal plate. Electrons are observed to be emitted from the metal plate, provided they are not faced with an electrostatic barrier of more than 0.613 V.
- What is the frequency of the photons? What is the corresponding energy of the photons?
  - What is the work function for this metal?
  - Explain qualitatively what would happen if the intensity of the light were cut down substantially.
  - Explain qualitatively what would happen if the frequency of the light were cut down substantially.

35. A particle has a wave function given by

$$\psi(x) = \begin{cases} \sqrt{2/a} \cos(\pi x/a) & \text{if } |x| < \frac{1}{2}a \\ 0 & \text{otherwise.} \end{cases}$$

- What is the most likely place to find the particle?
- If the position of the particle is measured, what is the probability that it will be found at  $0 < x < \frac{1}{6}a$ . Some possibly useful formulas can be found below.

$$\int \cos(Ax) dx = \sin(Ax)/A, \quad \int \cos^2(Ax) dx = x/2 + \sin(2AX)/4A,$$

$$\cos(0) = \sin\left(\frac{1}{2}\pi\right) = 1,$$

$$\cos\left(\frac{1}{3}\pi\right) = \sin\left(\frac{1}{6}\pi\right) = \frac{1}{2},$$

$$\cos\left(\frac{1}{2}\pi\right) = \sin(0) = 0,$$

$$\cos\left(\frac{1}{6}\pi\right) = \sin\left(\frac{1}{3}\pi\right) = \frac{\sqrt{3}}{2}.$$

**Part V: Calculation (new material): [60 points]**

Choose **three** of the following four questions and perform the indicated calculations (20 points each)

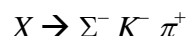
36. Thermonuclear weapons contain the radioactive isotope  ${}^3\text{H}$ , which has a half-life of 12.33 years and an atomic mass of 3.016 u.

- What is the decay rate  $\lambda$  for this isotope?
- If I have one gram of  ${}^3\text{H}$ , how many atoms do I have?
- What is the rate of decay for one gram of  ${}^3\text{H}$ ? You may leave your answer in decays/year, if you want.
- How long do we have to wait before that 1 g of  ${}^3\text{H}$  becomes 0.1 g of  ${}^3\text{H}$ , due to radioactive decay?

37. Photocopied with the equation on the next page is a portion of Appendix A from the text.  ${}^{50}\text{V}$  is an unstable nucleus which may have multiple decay modes.

- What would be the resulting isotope if this isotope underwent  $\beta^-$  decay? What if it underwent electron capture? What if it underwent  $\alpha$ -decay?
- What is the  $Q$ -value for each of these processes? Which of these modes is allowed or excluded?

38. There is a particle  $X$  which decays by strong interactions as follows:



The  $\Sigma^-$  is a baryon, and the other two are mesons.

The spin and strangeness of the other particles are listed at right. The charges are implied by their names.

- What is the charge and strangeness of the  $X$  particle?
- Is it a baryon, anti-baryon, or a meson?
- Is it a fermion or a boson?
- What, if anything, can you conclude about the mass of the  $X$ ?

All masses in $\text{MeV}/c^2$			
<u>Name</u>	<u>Mass</u>	<u>Spin</u>	<u>Strange</u>
$\Sigma^-$	1197	$\frac{1}{2}$	-1
$K^-$	495	0	-1
$\pi^+$	135	0	0

39. A certain black hole is discovered to have a Schwarzschild radius of 70.0 km.

- What is the mass of the black hole?
- Hydrogen atoms normally give off radiation with a wavelength of 21.0 cm. If the waves from hydrogen atoms near the black hole produce radiation with a wavelength observed at 28.0 cm, how far is the hydrogen from the black hole?

## Equations

Photoelectric effect:  $eV_{\max} = hf - \phi$

Basic Masses:  $u = 931.494 \text{ MeV} / c^2 = 1.661 \times 10^{-27} \text{ kg}$        $N_A = 6.022 \times 10^{23}$

Nuclear Decay:  $2m_e c^2 = 1.02200 \text{ MeV}$ ,       $M_{\text{He}} = 4.002602 \text{ u}$

Planck's Constants:  $h = 6.626 \times 10^{-34} \text{ J} \cdot \text{s} = 4.136 \times 10^{-15} \text{ eV} \cdot \text{s}$   
 $\hbar = 1.055 \times 10^{-34} \text{ J} \cdot \text{s} = 6.582 \times 10^{-16} \text{ eV} \cdot \text{s}$

Newton's Constant:  $G = 6.673 \times 10^{-11} \text{ m}^3 / \text{kg} / \text{s}^2$

Gravitational time dilation & Red-shift:  $\tau = t \sqrt{1 - \frac{2GM}{c^2 r}}$

Gravitational Red-shift:  $\lambda = \lambda_0 \left(1 - \frac{2GM}{c^2 r}\right)^{-1/2}$       Schwarzschild radius:  $R_s = \frac{2GM}{c^2}$

## Isotope Masses