

ANSWERS

1	<p>We use $\vec{F}_B = q\vec{v} \times \vec{B}$. Consider a three-dimensional coordinate system with the xy plane in the plane of this page, the $+x$ direction toward the right edge of the page and the $+y$ direction toward the top of the page. Then, the z axis is perpendicular to the page with the $+z$ direction being upward, out of the page. The magnetic field is directed in the $+x$ direction, toward the right.</p> <p>(a) When a proton (positively charged) moves in the $+y$ direction, the right-hand rule gives the direction of the magnetic force as into the page or in the $-z$ direction.</p> <p>(b) With velocity in the $-y$ direction, the right-hand rule gives the direction of the force on the proton as out of the page, in the $+z$ direction.</p> <p>(c) When the proton moves in the $+x$ direction, parallel to the magnetic field, the magnitude of the magnetic force it experiences is $F = qvB \sin(0^\circ) = 0$. The magnetic force is zero in this case.</p>	<p>Note: For this assignment, values of certain parameters may vary.</p>
2	<p>We first find the speed of the electron from the isolated system model:</p> $(\Delta K + \Delta U)_i = (\Delta K + \Delta U)_f \rightarrow \frac{1}{2}mv^2 = e\Delta V:$ $v = \sqrt{\frac{2e\Delta V}{m}} = \sqrt{\frac{2(1.60 \times 10^{-19} \text{ C})(2400 \text{ J/C})}{9.11 \times 10^{-31} \text{ kg}}} = 2.90 \times 10^7 \text{ m/s}$ <p>(a) $F_{B, \max} = qvB = (1.60 \times 10^{-19} \text{ C})(2.90 \times 10^7 \text{ m/s})(1.70 \text{ T})$ $= 7.90 \times 10^{-12} \text{ N}$</p> <p>(b) $F_{B, \min} = 0$ occurs when \vec{v} is either parallel to or anti-parallel to \vec{B}.</p>	
3	<p>The force on a charged particle is proportional to the vector product of the velocity and the magnetic field:</p> $\vec{F}_B = q\vec{v} \times \vec{B} = (1.60 \times 10^{-19} \text{ C})[(2\hat{i} - 4\hat{j} + \hat{k})(\text{m/s}) \times (\hat{i} + 2\hat{j} - \hat{k}) \text{ T}]$ <p>Since $1 \text{ C} \cdot \text{m} \cdot \text{T/s} = 1 \text{ N}$, we can write this in determinant form as:</p> $\vec{F}_B = (1.60 \times 10^{-19} \text{ N}) \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ 2 & -4 & 1 \\ 1 & 2 & -1 \end{vmatrix}$ <p>Expanding the determinant as described in Equation 11.8, we have</p> $\vec{F}_{B,x} = (1.60 \times 10^{-19} \text{ N}) [(-4)(-1) - (1)(2)]\hat{i}$ $\vec{F}_{B,y} = (1.60 \times 10^{-19} \text{ N}) [(1)(1) - (2)(-1)]\hat{j}$ $\vec{F}_{B,z} = (1.60 \times 10^{-19} \text{ N}) [(2)(2) - (1)(-4)]\hat{k}$	<p>Again in unit-vector notation,</p> $\vec{F}_B = (1.60 \times 10^{-19} \text{ N})(2\hat{i} + 3\hat{j} + 8\hat{k})$ $= (3.20\hat{i} + 4.80\hat{j} + 12.8\hat{k}) \times 10^{-19} \text{ N}$ $ \vec{F}_B = (\sqrt{3.20^2 + 4.80^2 + 12.8^2}) \times 10^{-19} \text{ N}$ $= 13.2 \times 10^{-19} \text{ N}$

- 4 (a) The magnetic force acting on the electron provides the centripetal acceleration, holding the electron in the circular path. Therefore,

$$F = |q|vB \sin 90^\circ = m_e v^2 / r, \text{ or}$$

$$r = \frac{m_e v}{eB} = \frac{(9.11 \times 10^{-31} \text{ kg})(1.50 \times 10^7 \text{ m/s})}{(1.60 \times 10^{-19} \text{ C})(2.00 \times 10^{-3} \text{ T})}$$

$$= 0.0427 \text{ m} = \boxed{4.27 \text{ cm}}$$

- (b) The time to complete one revolution around the orbit (i.e., the period) is

$$T = \frac{\text{distance traveled}}{\text{constant speed}} = \frac{2\pi r}{v} = \frac{2\pi(0.0427 \text{ m})}{1.50 \times 10^7 \text{ m/s}} = \boxed{1.79 \times 10^{-8} \text{ s}}$$

- 5 (a) The magnetic force provides the centripetal force to keep the particle moving on a circle:

$$\sum F = ma \quad \rightarrow \quad qvB \sin 90.0^\circ = \frac{mv^2}{R} \quad [1]$$

and the kinetic energy of the particle is

$$K = \frac{1}{2}mv^2 \quad [2]$$

Both equations have the same term mv^2 in common:

From [1], $mv^2 = qvBR$, and from [2], $mv^2 = 2K$.

Setting these equal to each other gives

$$mv^2 = qvBR = 2K \quad \rightarrow \quad \boxed{v = \frac{2K}{qBR}}$$

- (b) From [1], we have $m = \frac{qBR}{v}$. Using our result from (a), we get

$$m = \frac{qBR}{v} = qBR \left(\frac{qBR}{2K} \right) = \boxed{\frac{q^2 B^2 R^2}{2K}}$$

- 6 (a) The boundary between a region of strong magnetic field and a region of zero field cannot be perfectly sharp, but we ignore the thickness of the transition zone. In the field the electron moves on an arc of a circle:

$$\sum F = ma: \quad |q|vB \sin 90^\circ = \frac{mv^2}{r}$$

$$\frac{v}{r} = \omega = \frac{|q|B}{m} = \frac{(1.60 \times 10^{-19} \text{ C})(10^{-3} \text{ N} \cdot \text{s/C} \cdot \text{m})}{9.11 \times 10^{-31} \text{ kg}}$$

$$= 1.76 \times 10^8 \text{ rad/s}$$

The time for one half revolution is, from $\Delta\theta = \omega\Delta t$,

$$\Delta t = \frac{\Delta\theta}{\omega} = \frac{\pi \text{ rad}}{1.76 \times 10^8 \text{ rad/s}} = \boxed{1.79 \times 10^{-8} \text{ s}}$$

- (b) The maximum depth of penetration is the radius of the path. The magnetic force cannot alter the kinetic energy of the electron.

Then,

$$v = \omega r = (1.76 \times 10^8 \text{ s}^{-1})(0.0200 \text{ m}) = 3.51 \times 10^6 \text{ m/s}$$

and

$$\begin{aligned} K &= \frac{1}{2}mv^2 = \frac{1}{2}(9.11 \times 10^{-31} \text{ kg})(3.51 \times 10^6 \text{ m/s})^2 \\ &= 5.62 \times 10^{-18} \text{ J} = \frac{5.62 \times 10^{-18} \text{ J}}{1.60 \times 10^{-19} \text{ J/eV}} = \boxed{35.1 \text{ eV}} \end{aligned}$$

- 7 (a) The name "cyclotron frequency" refers to the angular frequency or angular speed

$$\omega = \frac{qB}{m}$$

For protons,

$$\omega = \frac{(1.60 \times 10^{-19} \text{ C})(0.450 \text{ T})}{1.67 \times 10^{-27} \text{ kg}} = \boxed{4.31 \times 10^7 \text{ rad/s}}$$

- (b) The path radius is $R = \frac{mv}{Bq}$.

Just before the protons escape, their speed is

$$v = \frac{BqR}{m} = \frac{(0.450 \text{ T})(1.60 \times 10^{-19} \text{ C})(1.20 \text{ m})}{1.67 \times 10^{-27} \text{ kg}} = \boxed{5.17 \times 10^7 \text{ m/s}}$$

- 8 From the electron to travel undeflected, we require $F_B = F_e$, so

$$qvB = qE$$

where $v = \sqrt{\frac{2K}{m}}$ and K is kinetic energy of the electron. Then,

$$\begin{aligned} E = vB &= \sqrt{\frac{2K}{m}}B = \sqrt{\frac{2(750 \text{ eV})(1.60 \times 10^{-19} \text{ J/eV})}{9.11 \times 10^{-31} \text{ kg}}}(0.0150 \text{ T}) \\ &= \boxed{244 \text{ kV/m}} \end{aligned}$$

- (b) Solution to **What If?**

For a proton to be undeflected, its speed must be given by

$$v = \frac{E}{B}$$

The kinetic energy of the proton would then be

$$K = \frac{1}{2}mv^2 = \frac{mE^2}{2B^2}$$

- 9 (a) From $F = BIL \sin \theta$, the magnetic field is

$$B = \frac{F/L}{I \sin \theta} = \frac{0.120 \text{ N/m}}{(15.0 \text{ A}) \sin 90^\circ} = \boxed{8.00 \times 10^{-3} \text{ T}}$$

- (b) The magnetic field must be in the +z direction to produce a force in the $-y$ direction when the current is in the $+x$ direction.

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- (a) The magnetic force must be upward to lift the wire. For current in the south direction, the magnetic field must be **east** to produce an upward force, as shown by the right-hand rule in the figure.



- (b) $F_B = ILB \sin \theta$ with $F_B = F_g = mg$

$$mg = ILB \sin \theta \quad \text{so} \quad \frac{m}{L}g = IB \sin \theta \quad \rightarrow \quad B = \frac{m}{L} \frac{g}{I \sin \theta}$$

$$B = \frac{m}{L} \frac{g}{I \sin \theta} = \left(\frac{0.500 \times 10^{-3} \text{ kg}}{1.00 \times 10^{-2} \text{ m}} \right) \left(\frac{9.80 \text{ m/s}^2}{(2.00 \text{ A}) \sin 90.0^\circ} \right) = \boxed{0.245 \text{ T}}$$

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- (a) From the circumference of the loop, $2\pi r = 2.00 \text{ m}$, we find its radius to be $r = 0.318 \text{ m}$. The magnitude of the magnetic moment is then

$$\mu = IA = (17.0 \times 10^{-3} \text{ A}) [\pi (0.318)^2 \text{ m}^2] = \boxed{5.41 \text{ mA} \cdot \text{m}^2}$$

- (b) The torque on the loop is given by Equation 29.17, $\vec{\tau} = \vec{\mu} \times \vec{B}$, and its magnitude is

$$\tau = (5.41 \times 10^{-3} \text{ A} \cdot \text{m}^2)(0.800 \text{ T}) = \boxed{4.33 \text{ mN} \cdot \text{m}}$$

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- (a) $\tau = NBAI \sin \phi$

$$\tau = 100(0.800 \text{ T})(0.400 \times 0.300 \text{ m}^2) \times (1.20 \text{ A}) \sin 60^\circ$$

$$\tau = \boxed{9.98 \text{ N} \cdot \text{m}}$$

- (b) Note that ϕ is the angle between the magnetic moment and the \vec{B} field. The loop will rotate so as to align the magnetic moment with the \vec{B} field, **clockwise as seen looking down from a position on the positive y axis.**

