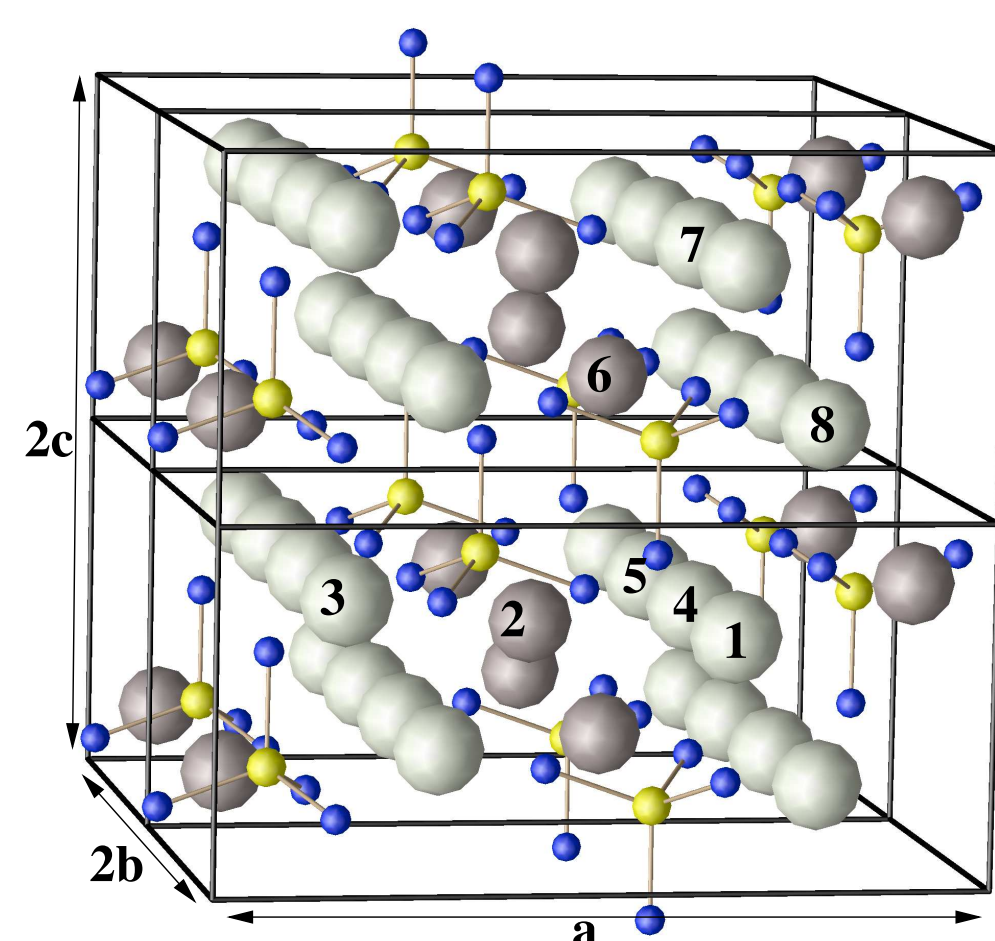


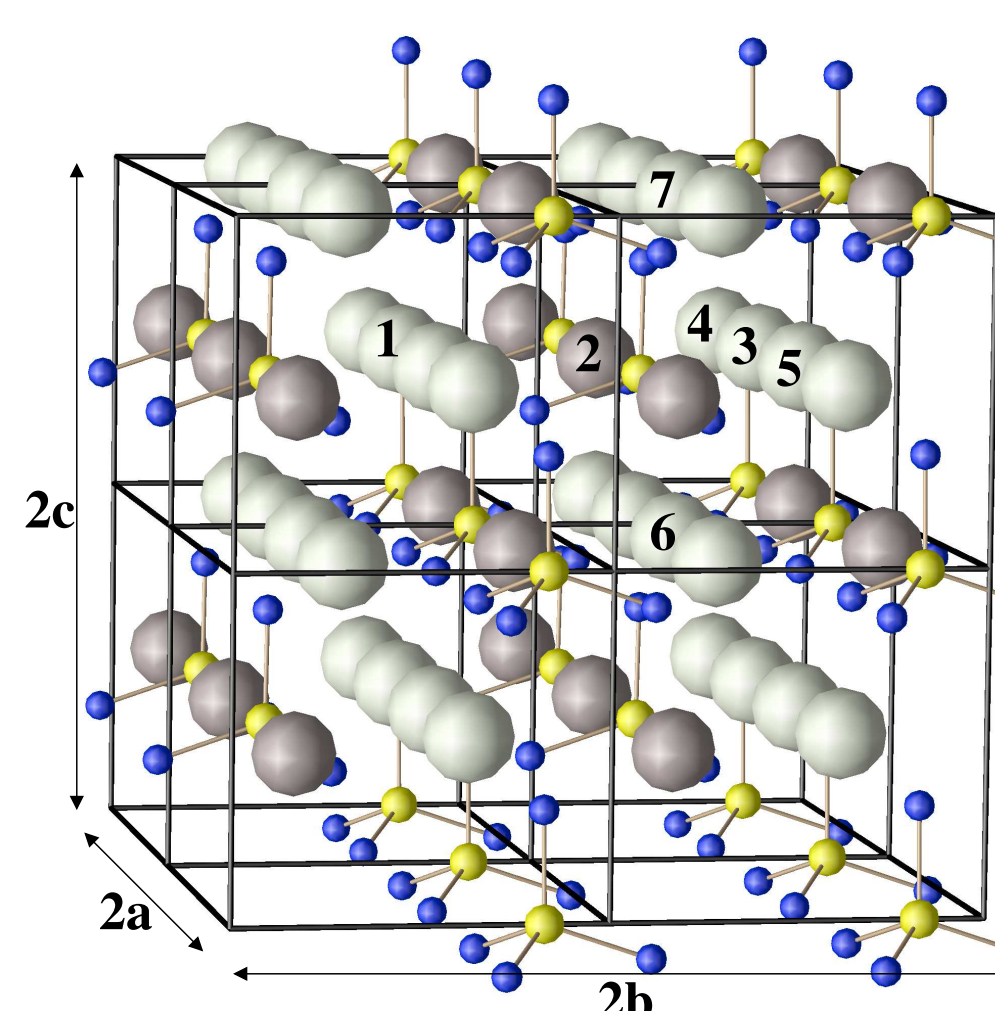
Introduction

- Solid-state lithium ion electrolytes such as Li_3PO_4 -based materials¹ are becoming increasingly important in batteries and related technologies.
- Li ion diffusion in crystalline γ - Li_3PO_4 has been measured to be slightly anisotropic with activation energies of 1.1–1.3 eV.² The activation energies can be reduced to 0.97 eV by N doping¹ and to 0.5 eV by admixture with Li_4SiO_4 .³
- In this work, first-principles calculations⁴ have been performed to model the migration energies for both vacancy and interstitial mechanisms of Li ions in γ - Li_3PO_4 and β - Li_3PO_4 . For extrinsic defects, activation energy E_A is the same as the migration energy of the defects, E_m . However, for intrinsic defects, using quasi-equilibrium statistical mechanics arguments,⁵ it follows that $E_A = E_m + E_f/2$, where E_f is the formation energy of the vacancy-interstitial pair.

Crystal structures



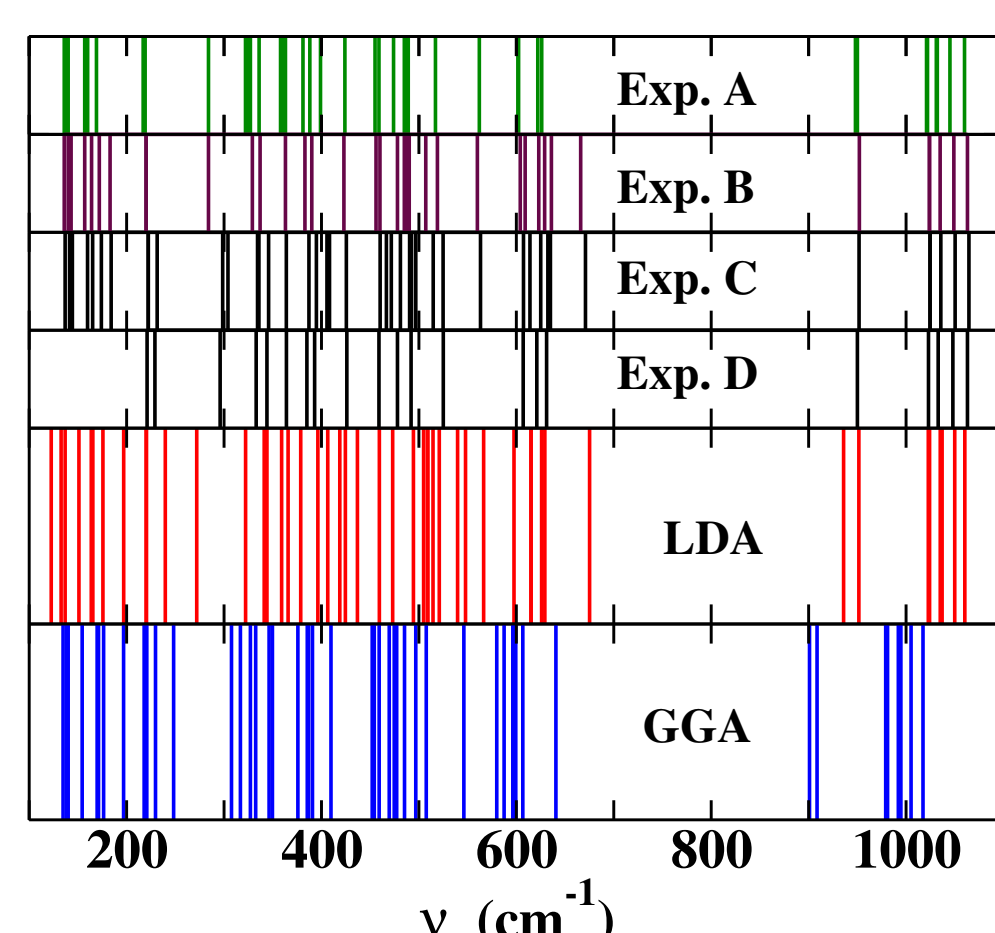
γ - Li_3PO_4 Space group: Pnma
Metastable at room temperature; experimentally measured. The Li ions are located on two crystallographically different sites indicated with different shadings (gray and dark balls) in the figure. Using the Wyckoff labels, the *d* site accounts for 8 equivalent atomic sites and the *c* site accounts for 4 equivalent atomic sites per unit cell. The P and O ions are indicated by small balls and sticks (colored yellow and blue respectively).



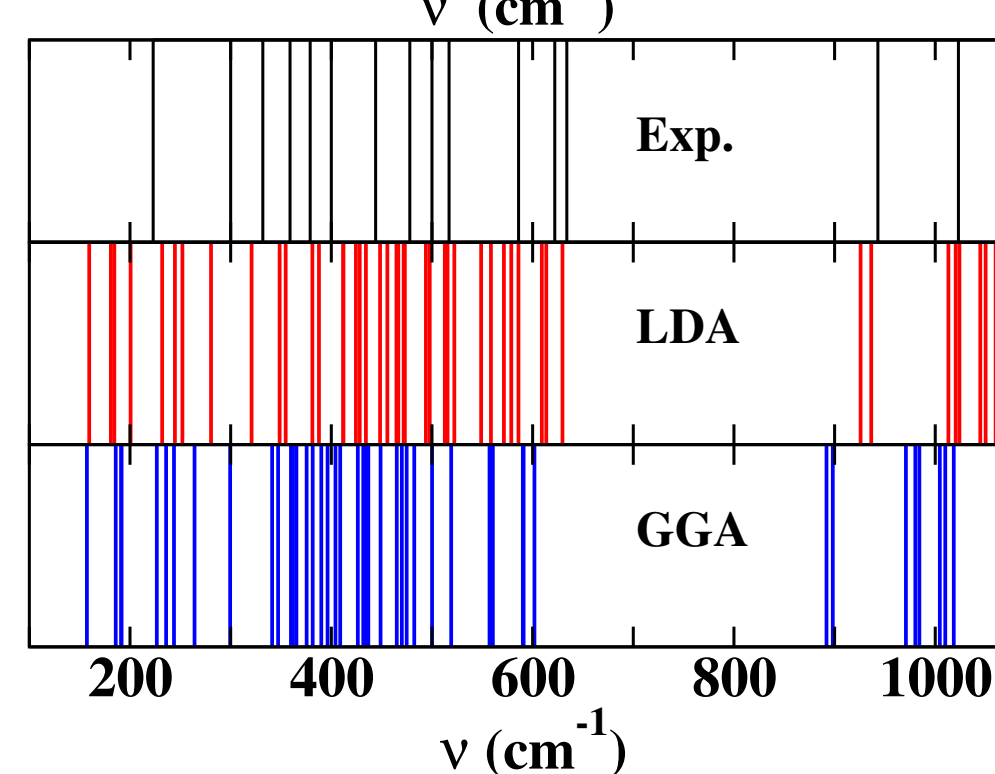
β - Li_3PO_4 Space group: Pmn2₁
Low-temperature phase and energetically more stable than γ -phase. Two crystallographically distinct Li sites are also indicated with different shadings in the figure. Using the Wyckoff labels, the *b* site accounts for 4 equivalent atomic sites and the *a* site accounts for 2 equivalent atomic sites per unit cell. Our calculations verify that the β form is energetically more stable: $E_\gamma - E_\beta = 0.03(0.01)$ eV/ Li_3PO_4 for LDA (GGA) calculations.

Raman spectra

LDA calculations show better agreement with experimental spectra than GGA; simulation results in this poster are presented for the LDA functional unless otherwise specified.

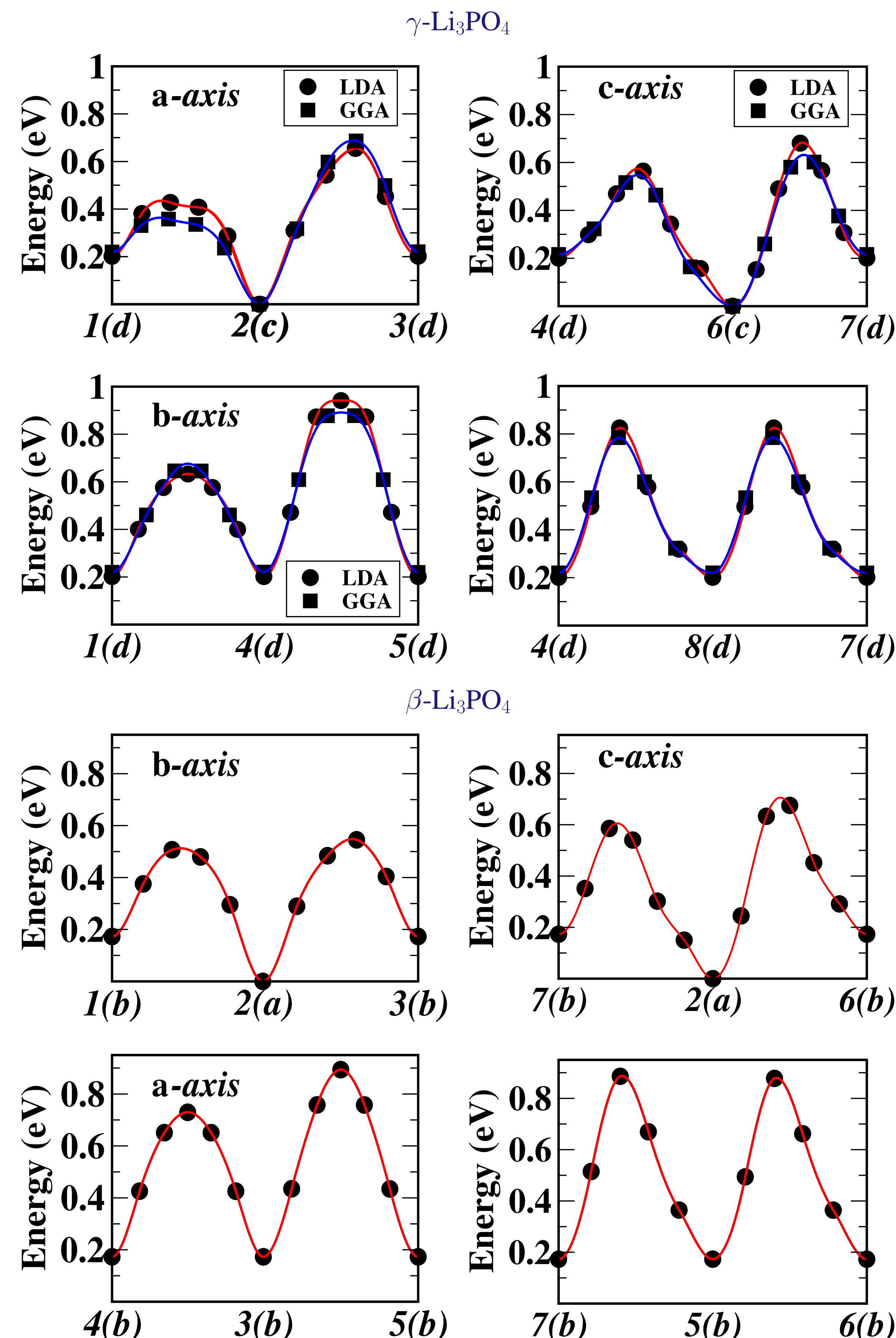


Raman active modes of γ - Li_3PO_4 , comparing experimental results with LDA and GGA calculations. Experiment A (from Ref. 6) was measured at room temperature (RT). Experiment B and C (from Ref. 7) were measured at RT and liquid nitrogen temperature (LNT), respectively. Experiment D (from Ref. 8) was measured at LNT.



Raman active modes of β - Li_3PO_4 , comparing experimental results with LDA and GGA calculations. Experimental data (from Ref. 8) were measured at LNT.

Vacancy mechanism



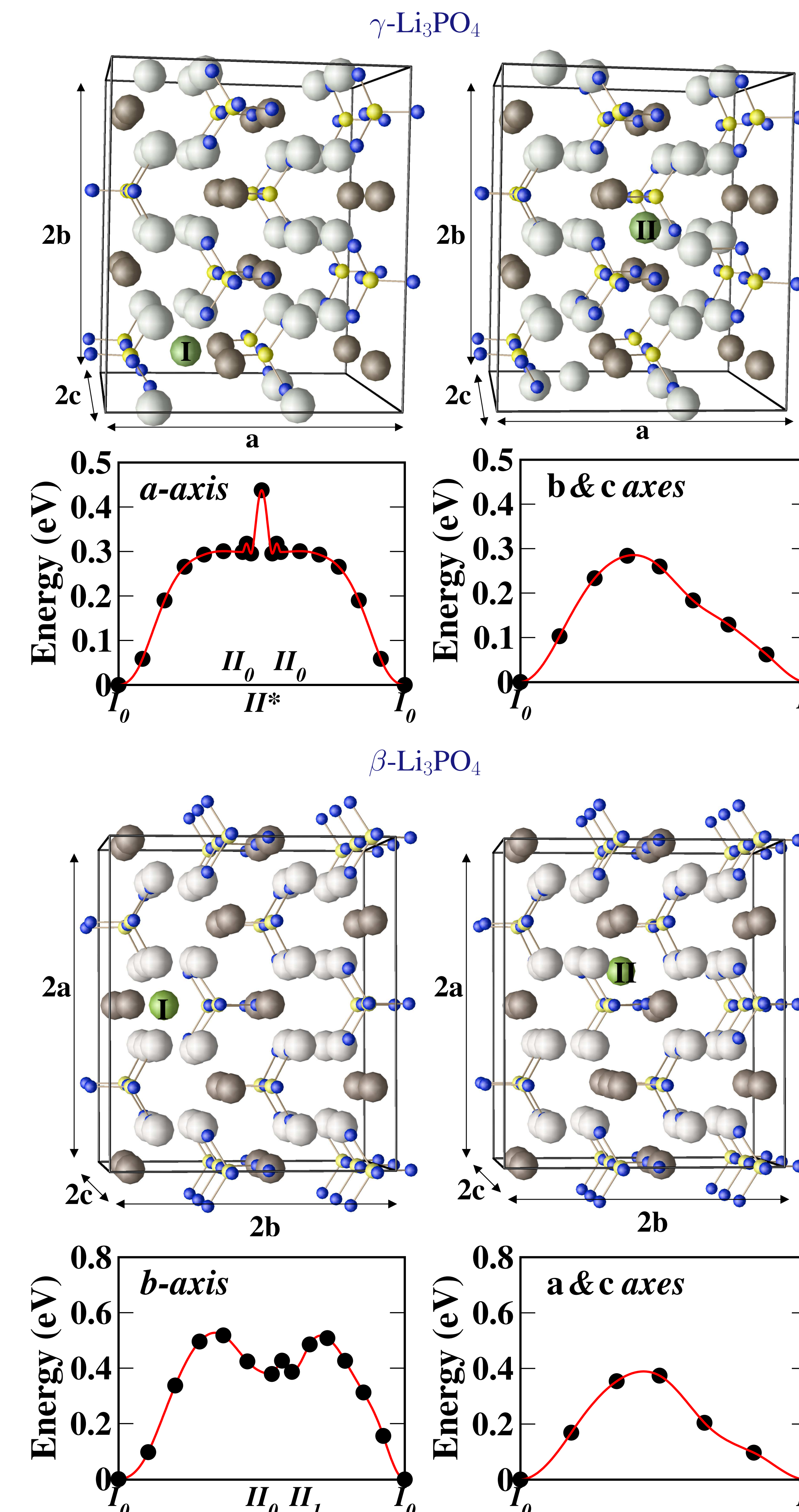
Energy path diagrams for various vacancy migration paths in crystalline Li_3PO_4 , showing minimal barriers of 0.62 eV along the *c*-axis path for the γ form and 0.55 eV along the *b*-axis path for the β form. These barriers are 0.3 eV lower than the measured activation energy for vacancy-rich $\text{Li}_{2.88}\text{PO}_{3.73}\text{N}_{0.14}$,¹ where oxygen-vacancies may affect the migration barrier.

Intrinsic defects

The formation energies of interstitial-vacancy pairs are found to be $E_f(\gamma) = 1.7$ eV and $E_f(\beta) = 2.1$ eV. Estimating the intrinsic activation energy as $E_A = E_m(\text{interstitial}) + E_f/2$, we obtain good agreement with experiment.²

Crystal	Net direction	Experiment (eV)	This work (eV)
γ - Li_3PO_4	a	1.23	1.1
	b	1.14	1.1
	c	1.14	1.1
β - Li_3PO_4	b		1.6
	a		1.4
	c		1.4

Interstitial mechanism



Interstitial migration paths show the most efficient ion transport mechanism for both γ - and β - Li_3PO_4 , with computed migration barriers of 0.3–0.5 eV, in good agreement with the measured 0.5 eV activation energy of extrinsic interstitials for Li_4SiO_4 - Li_3PO_4 solid solutions.³ Structural diagrams show meta-stable interstitial sites *I* and *II* located in the two distinct void channels for both crystals.

Reference

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