

Electrolyte properties of $\text{Li}_4\text{P}_2\text{S}_6$ -- Simulations and comparison with experiment; Contrast with simulations of Na analog*

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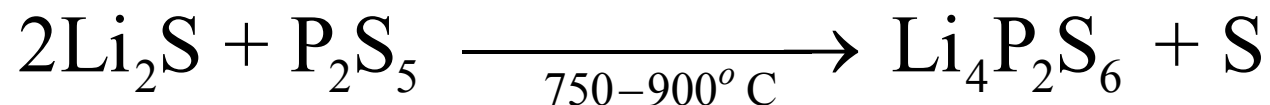
$\text{Li}_4\text{P}_2\text{S}_6 / \text{Na}_4\text{P}_2\text{S}_6$

- Why--**
- Search for ideal solid electrolyte materials for all-solid state batteries
 - $\text{Li}_4\text{P}_2\text{S}_6$ reported by Mercier et al., J. Solid State Chem. **43**, 151-164 (1982); hexagonal structure with disorder on the P sites
 - $\text{Li}_4\text{P}_2\text{S}_6$ frequently identified as unintended constituent of solid electrolyte preparations; relatively stable in air
 - $\text{Na}_4\text{P}_2\text{S}_6$ recently report by Kuhn et al., ZAAC **640**, 689-692 (2014); related ordered structure

- What--** Experimental results for $\text{Li}_4\text{P}_2\text{S}_6$ and computation results for $\text{Li}_4\text{P}_2\text{S}_6$ and $\text{Na}_4\text{P}_2\text{S}_6$:
- Structural analysis
 - Transport properties
 - Interfaces with Li or Na metal

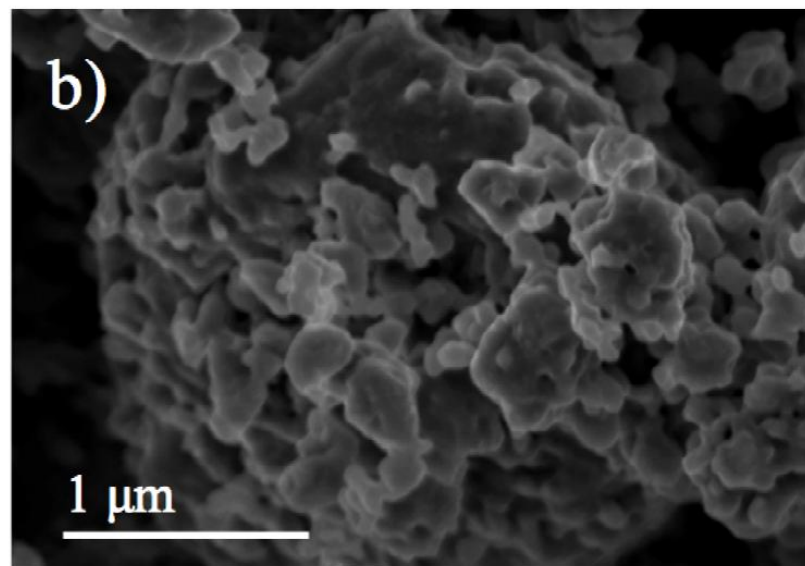
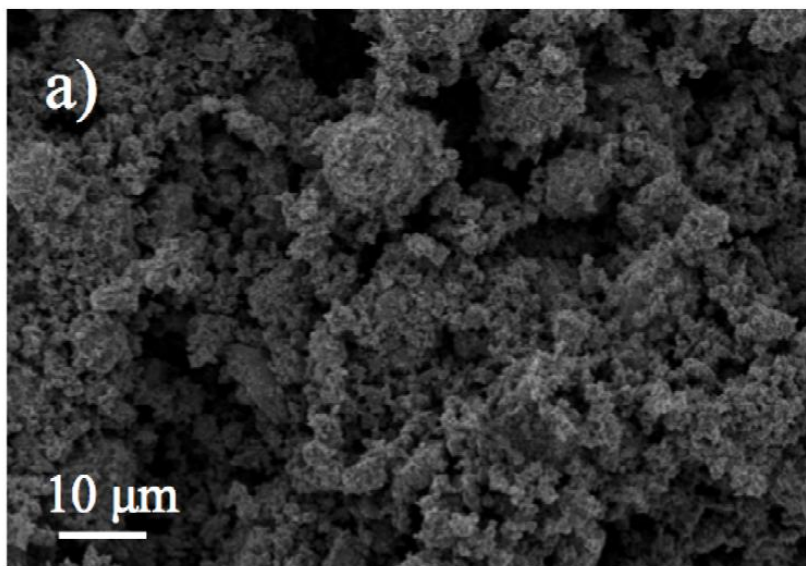


Synthesis:



Sulfur removed by treatment with solvent; powder sample prepared for electrochemical applications using ball milling.

Scanning Electron Micrograph of prepared sample:



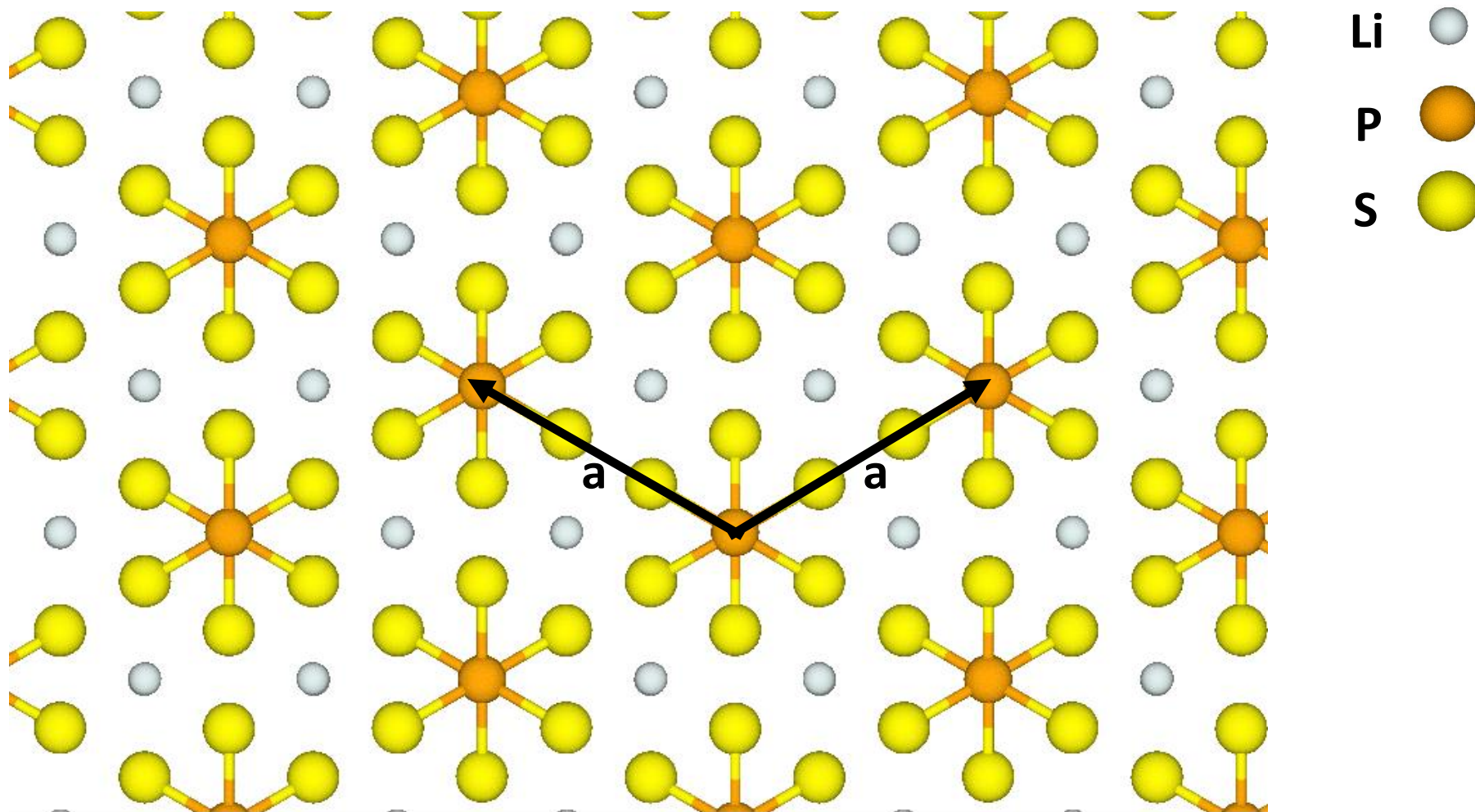
Computational methods

- Density functional theory with LDA
- PAW formalism using datasets generated with **ATOMPAW** code (Holzwarth et al. *CPC* **135**, 329 (2001)) <http://pwpaw.wfu.edu>
- Electronic structure calculations performed using **QUANTUM ESPRESSO** and **ABINIT** codes. (Giannozzi et al. *JPCM* **21**, 394402 (2009); <http://www.quantum-espresso.org>, Gonze et al., *CPC* **180**, 2582 (2009)); <http://www.abinit.org>
- Plane wave expansion for wave functions with $|\mathbf{k} + \mathbf{G}|^2 \leq 64 \text{ Ry}$
- Brillouin zone integration mesh of 0.003 bohr^{-3}
- Ion migration energies estimated with Nudged Elastic Band (NEB) method. (Hinkleman et al. *JCP* **113**, 9901 & 9978 (2000))
- Visualization software: **Xcrysden**, **VESTA**, and **CrystalMaker**
- X-ray powder diffraction simulated using **Mercury**
- Neutron powder diffraction simulated using **GSAS**



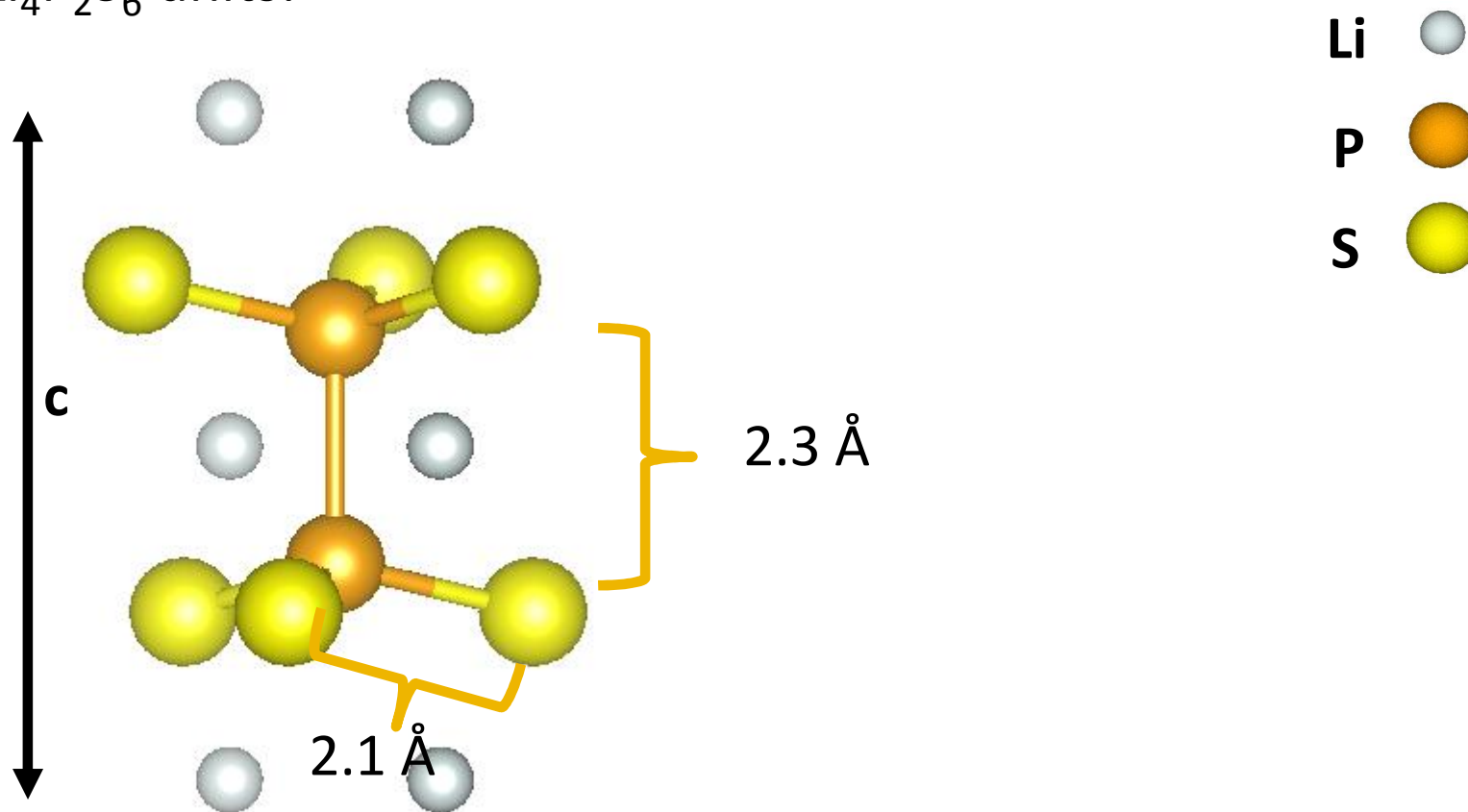
Crystal structure of $\text{Li}_4\text{P}_2\text{S}_6$: Space Group $P6_3/mcm$ (#193)

Projection on to hexagonal plane:



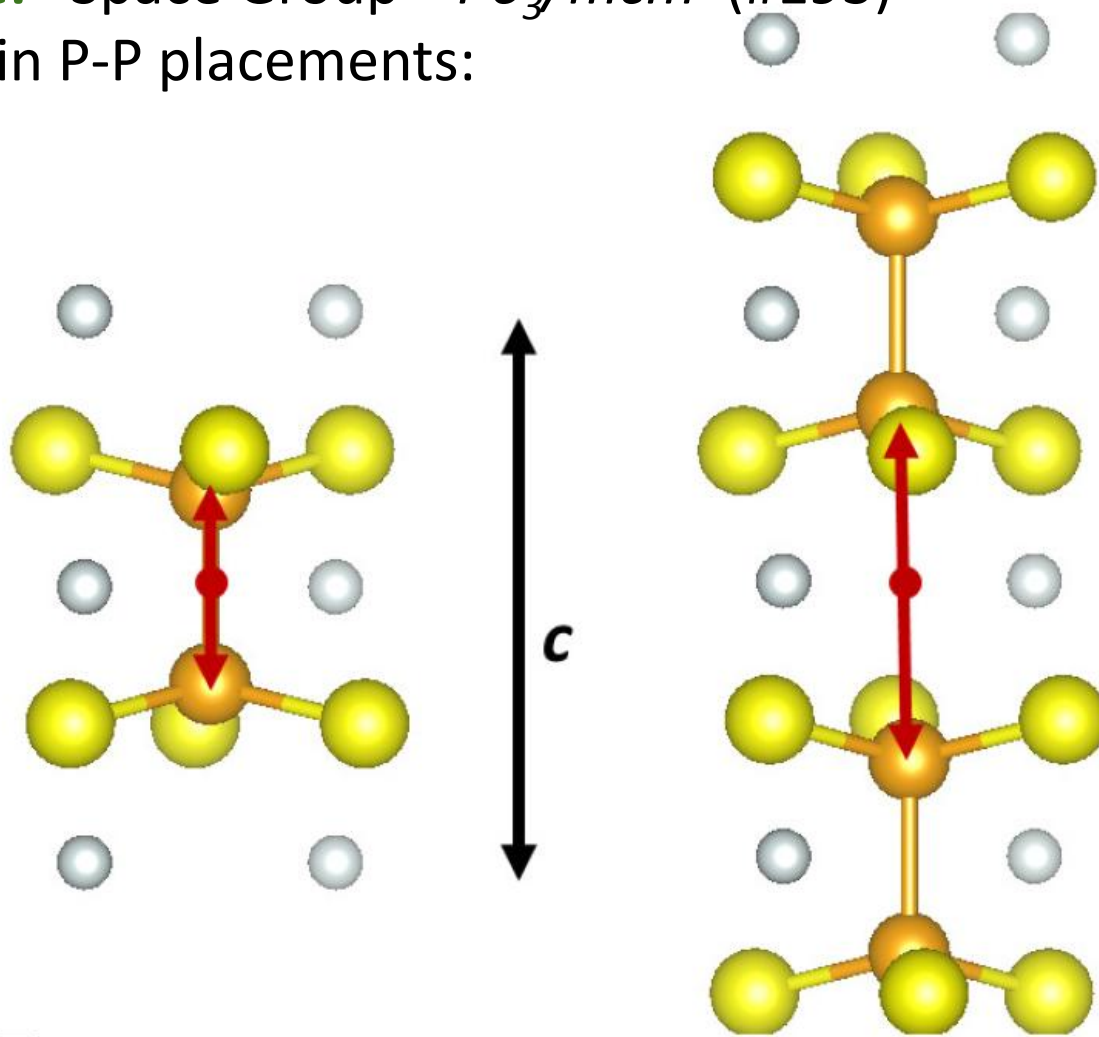
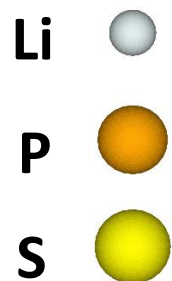
Crystal structure of $\text{Li}_4\text{P}_2\text{S}_6$: Space Group $P6_3/mcm$ (#193)

$\text{Li}_4\text{P}_2\text{S}_6$ units:



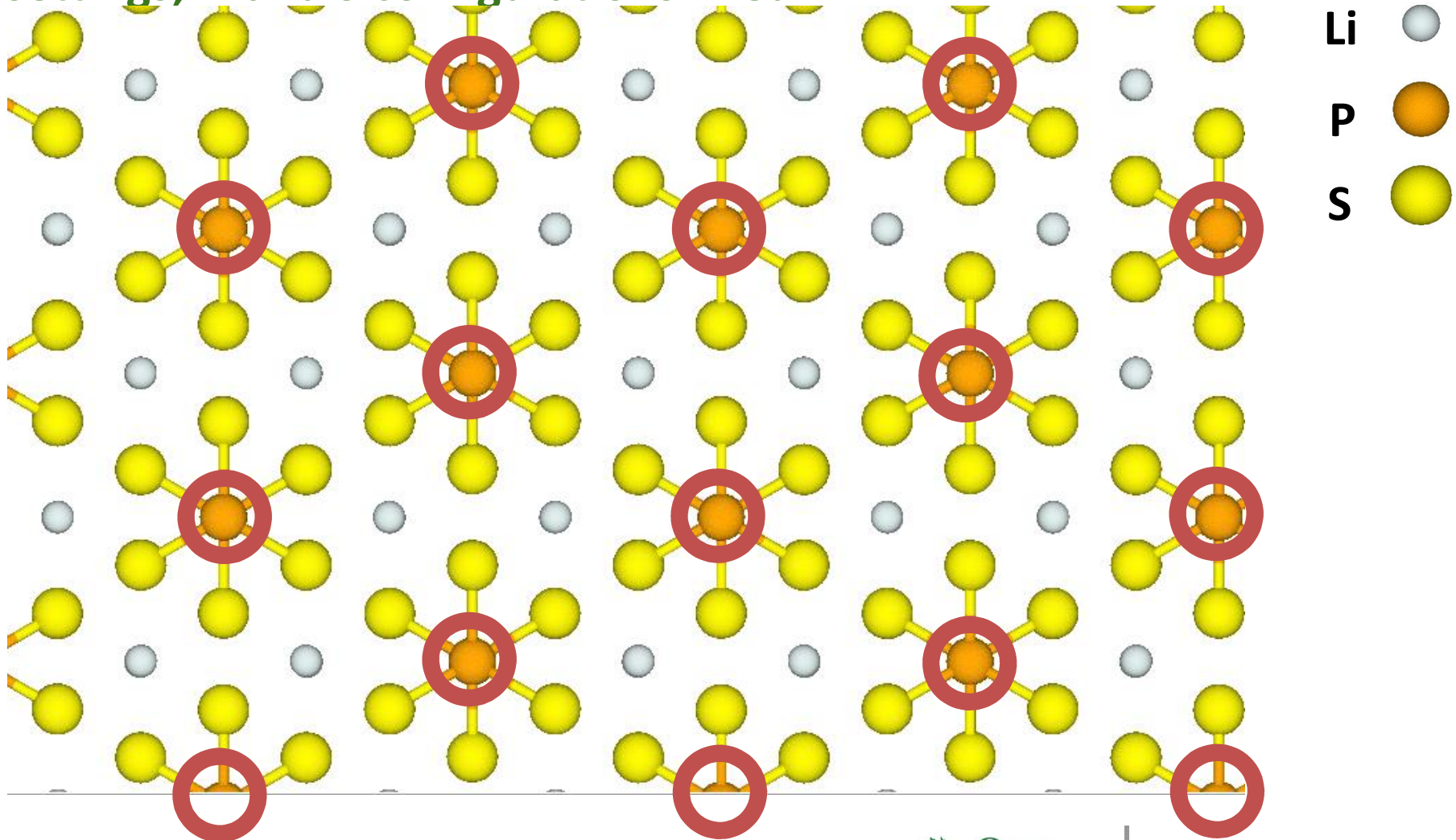
Crystal structure: Space Group $P6_3/mcm$ (#193)

Disorder in P-P placements:



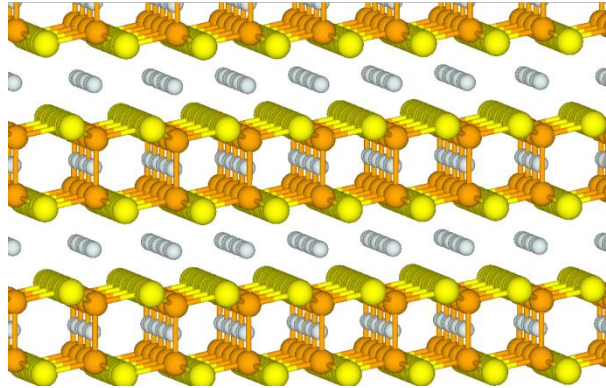
$$P_{\uparrow} \equiv \pm z_P c \quad P_{\downarrow} \equiv \pm \left(\frac{1}{2} - z_P \right) c$$

Structural variation can be mapped on to a two-dimensional hexagonal lattice with each P configuration taking $P\uparrow$ or $P\downarrow$ settings; Li and S configurations fixed



Examples:

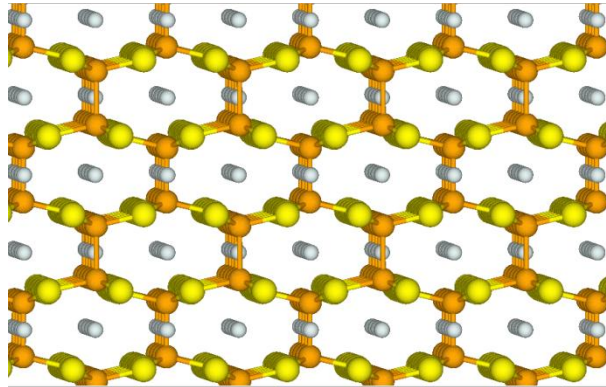
Structure "b"
 $P\bar{3}1m$



$$\Delta E = 0.03 \text{ eV}$$

100% P↑

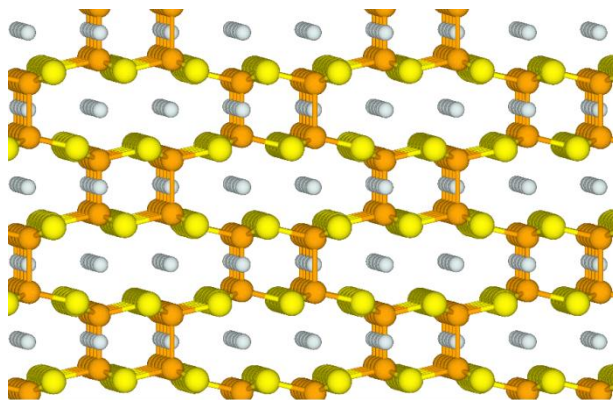
Structure "c"
 $Pn\bar{3}m$



$$\Delta E = 0$$

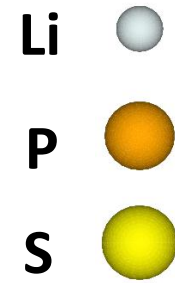
50% P↑
50% P↓

Structure "d"
 $Pnma$



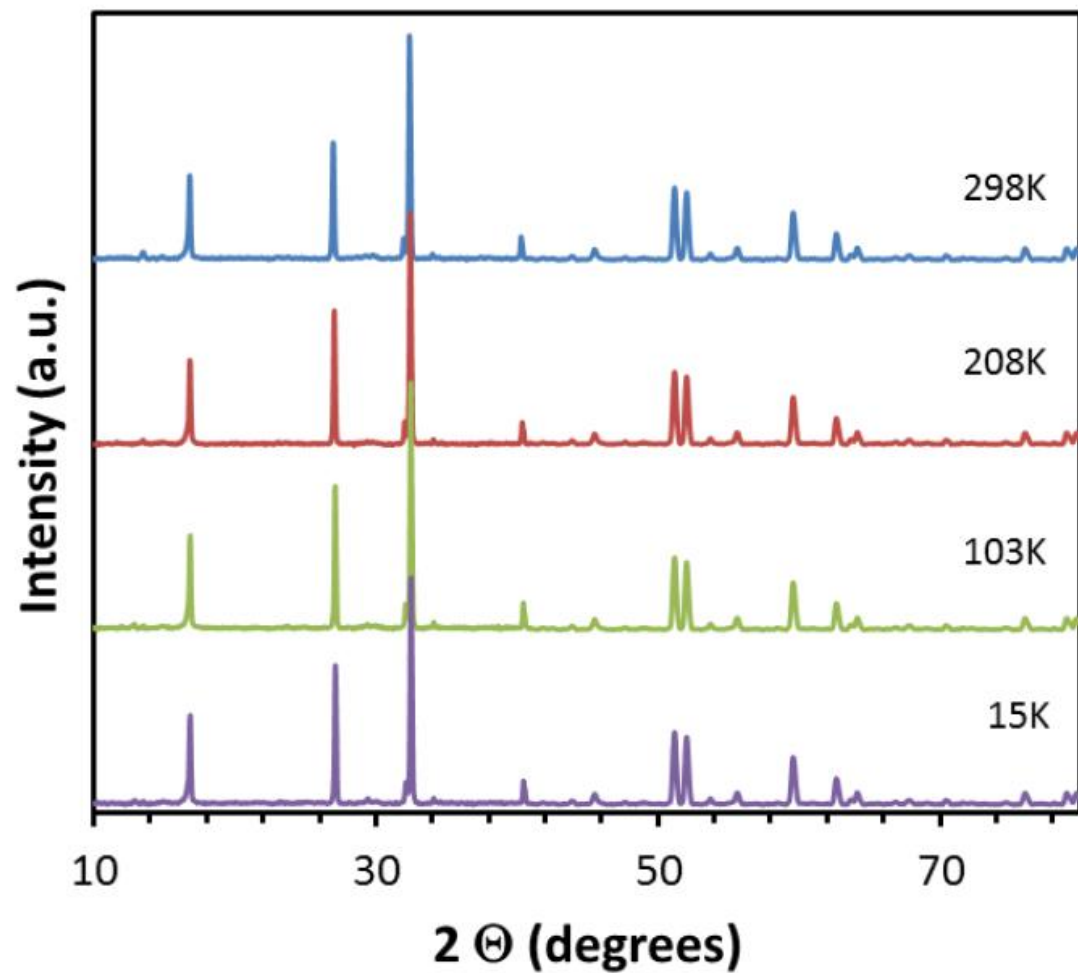
$$\Delta E = 0$$

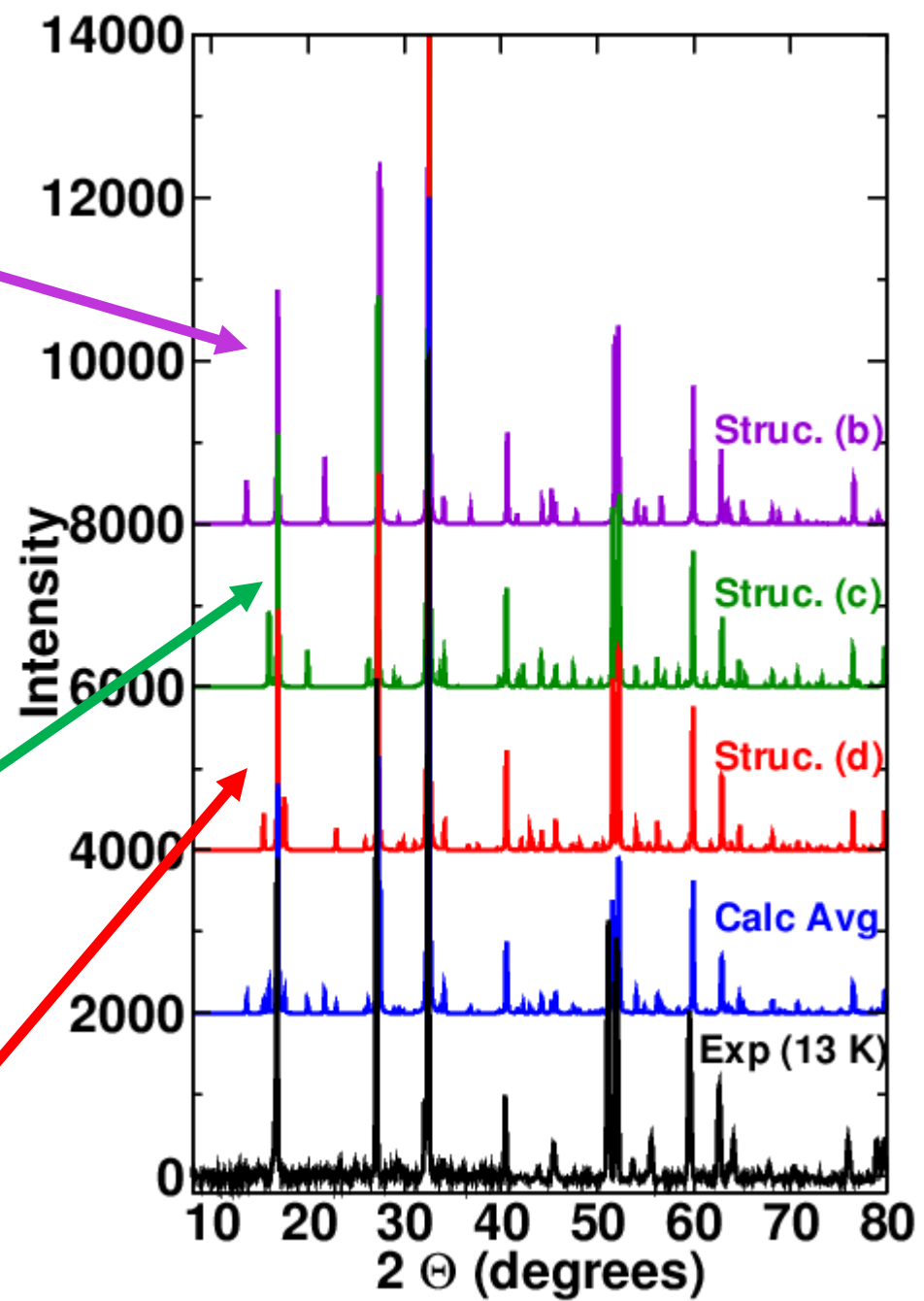
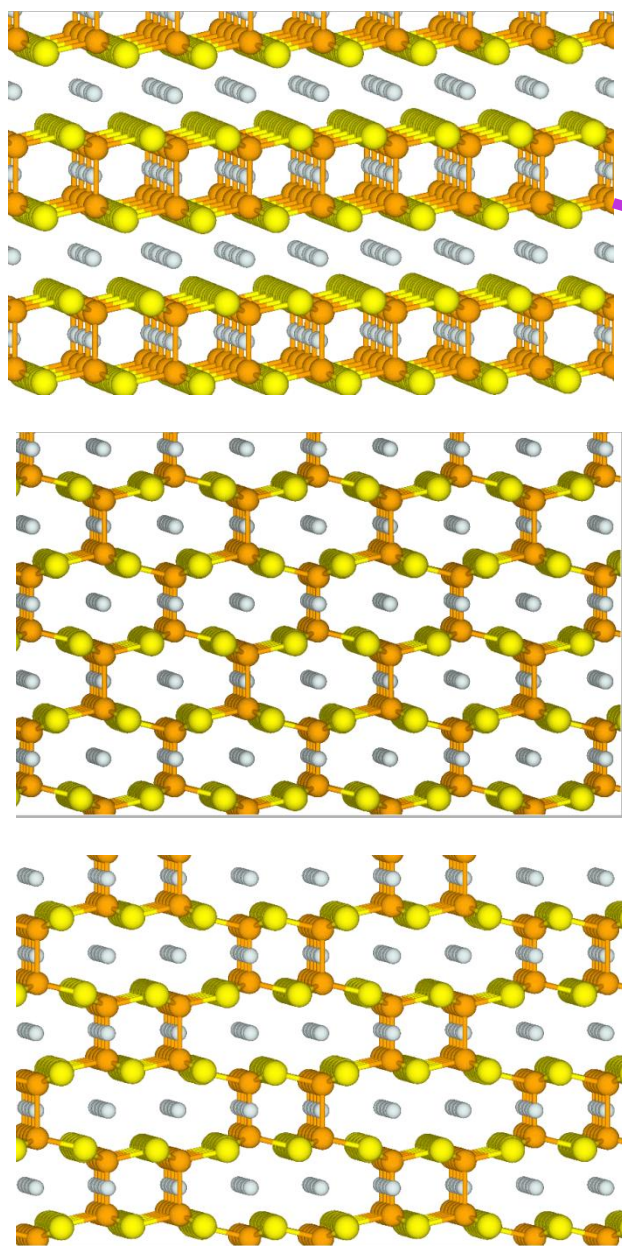
50% P↑
50% P↓



Two model configurations of disordered ground state structure

Temperature ⁱⁿ dependence of X-ray powder diffraction

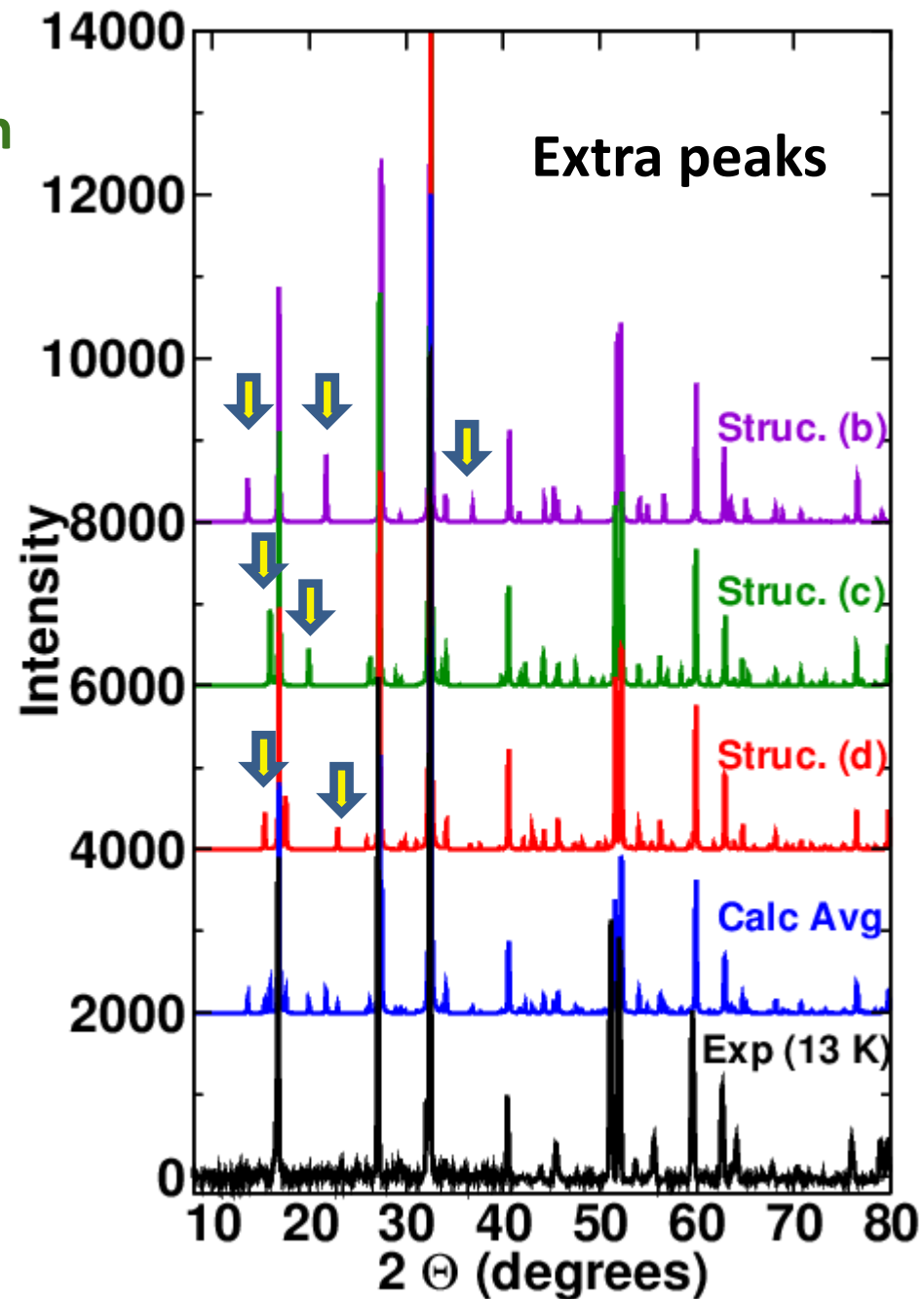




Comparison of 15 K X-ray data with simulation

Note: simulations
scaled by 102%
to compensate
for systematic
LDA error.

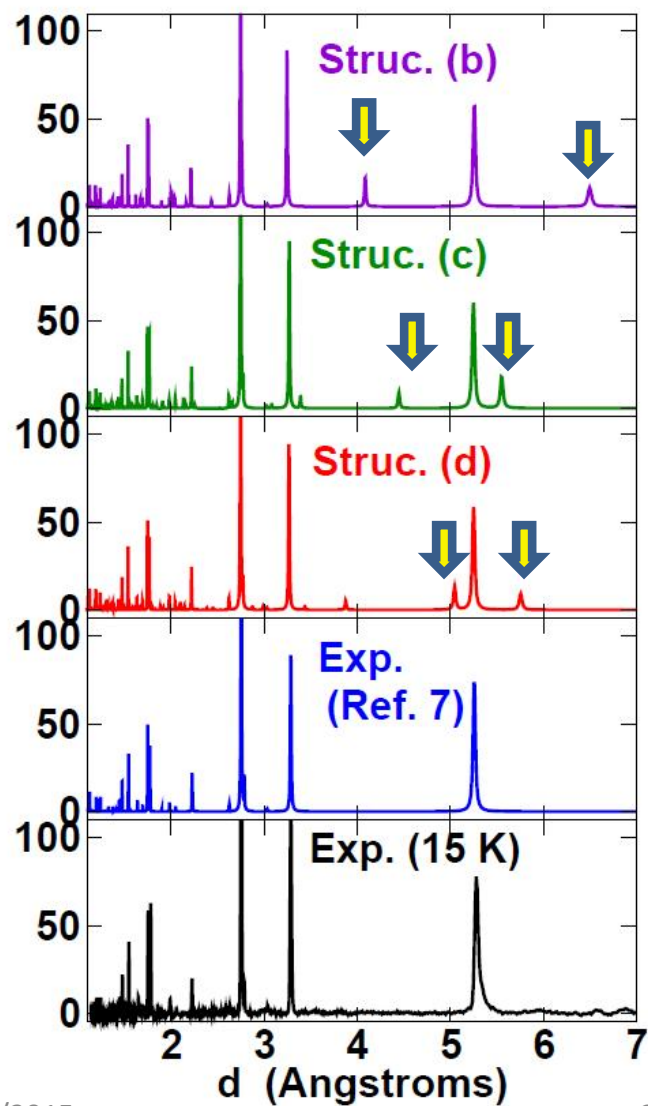
Simulations consistent
with incoherent average
over all $P\uparrow$ and $P\downarrow$
configurations



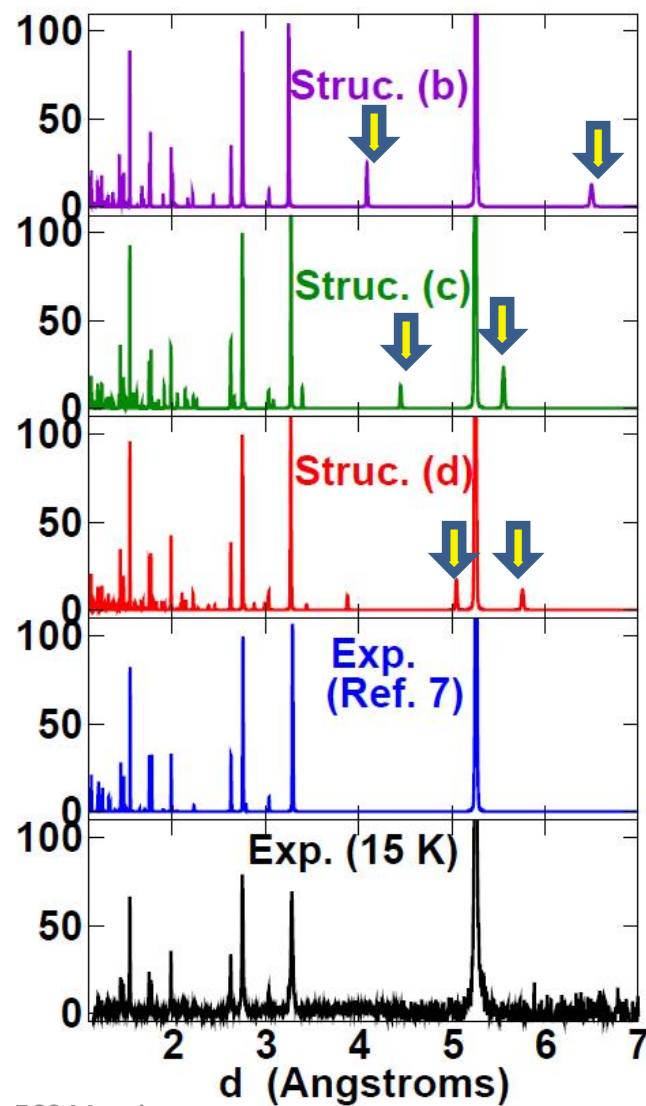
In terms of diffracting plane spacing:

$$d = \lambda / (2\sin\Theta)$$

X-ray spectrum



Neutron spectrum



Structural parameters

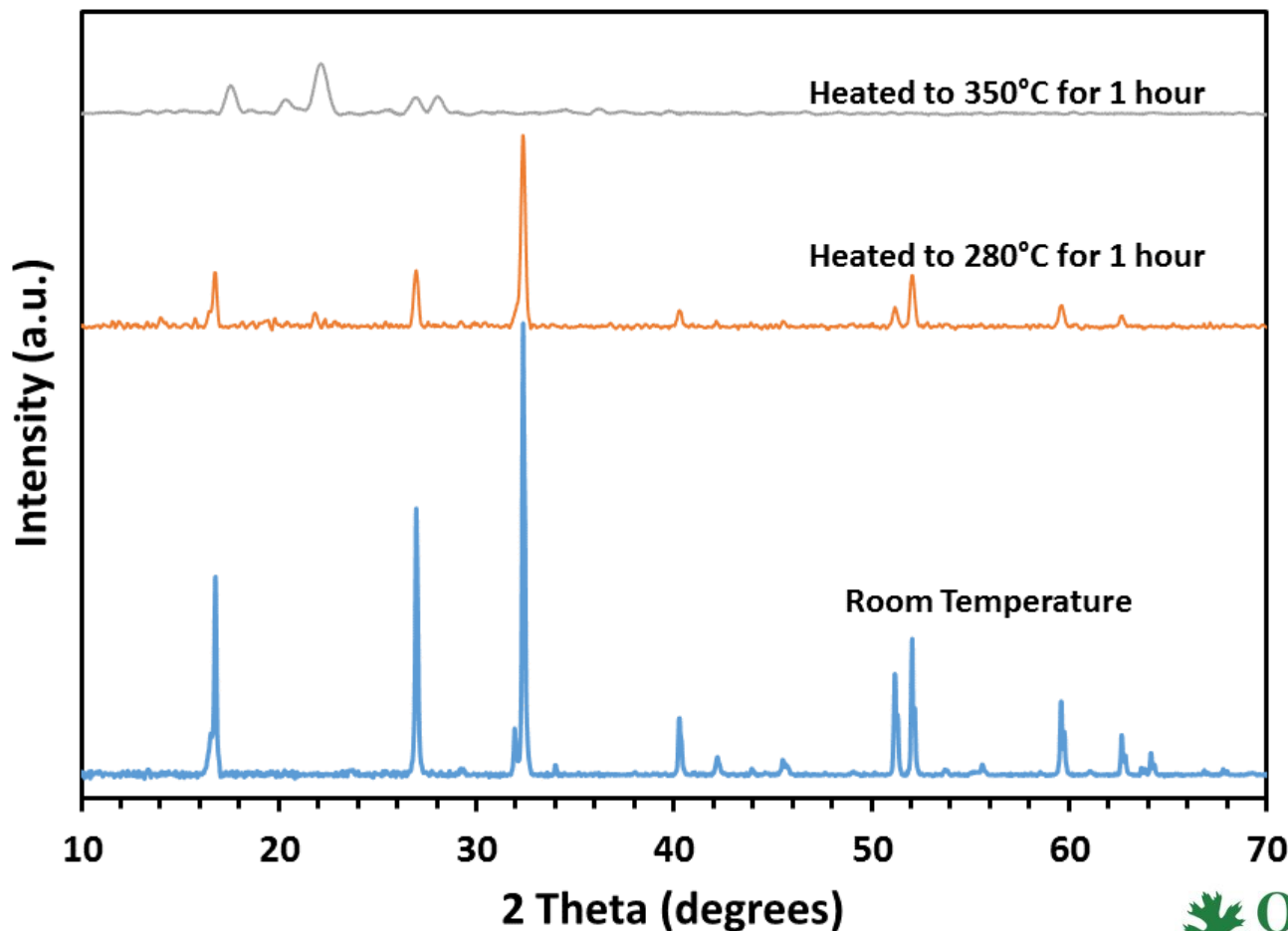
	a (Å)	c (Å)	z_p	z_s	
Exp. 293K (X-ray)*	6.070	6.557	0.1715	0.3237	} Hood <i>et al.</i> **
Exp. 300K (X-ray)	6.075	6.597	0.172	0.324	
Exp. 300K (neutron)	6.075	6.595	0.173	0.326	
Exp. 15K (X-ray)	6.051	6.548	0.172	0.324	
Exp. 15K (neutron)	6.055	6.553	0.172	0.326	
Calc. structure "b"	6.07	6.50	0.18	0.33	} with 102% LDA corr.
Calc. structure "c"	6.06	6.54	0.17	0.33	
Calc. structure "d"	6.06	6.54	0.17	0.33	

*Mercier *et al.*, J. Solid State Chem. 43, 151 (1982)

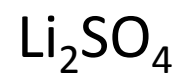
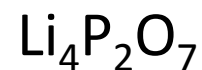
**Hood *et al.*, submitted to SSI (2015)



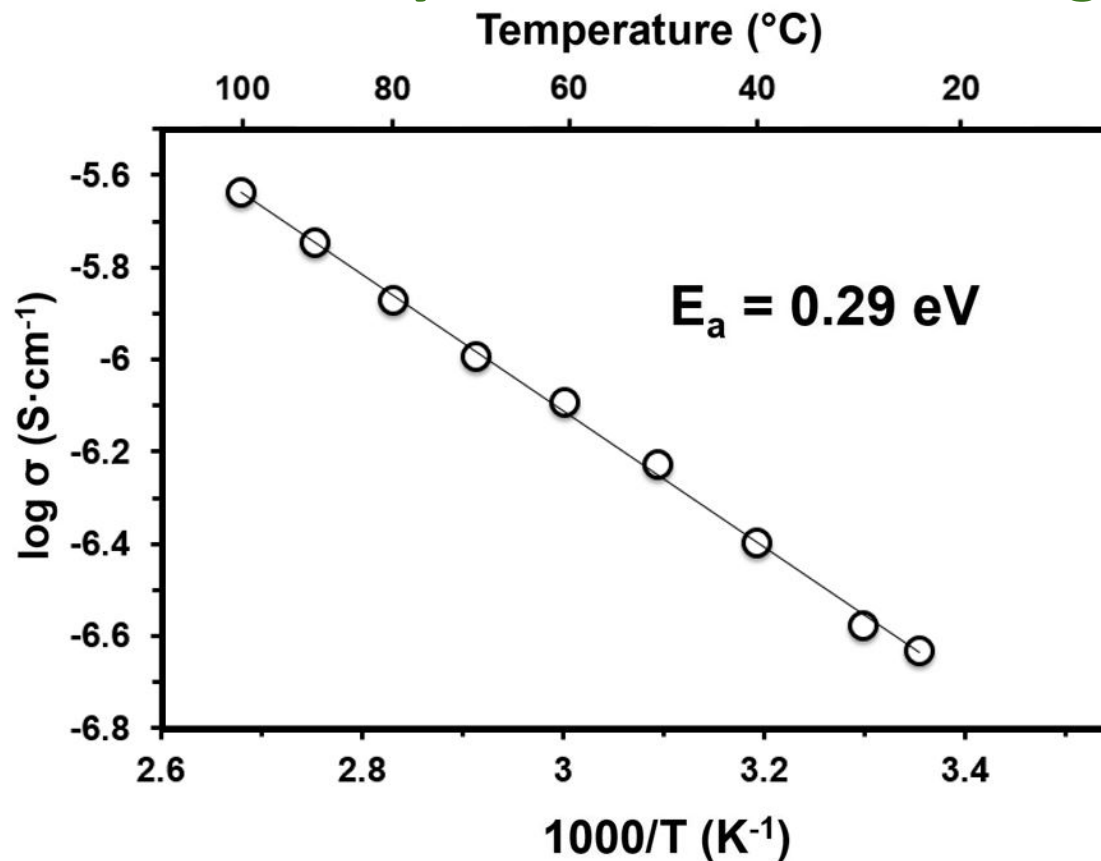
Stability: $\text{Li}_4\text{P}_2\text{S}_6$ is much less reactive than other lithium thio-phosphates, but it decomposes in air, especially at higher temperature



Decomposition products:



Ionic conductivity and Activation Energy






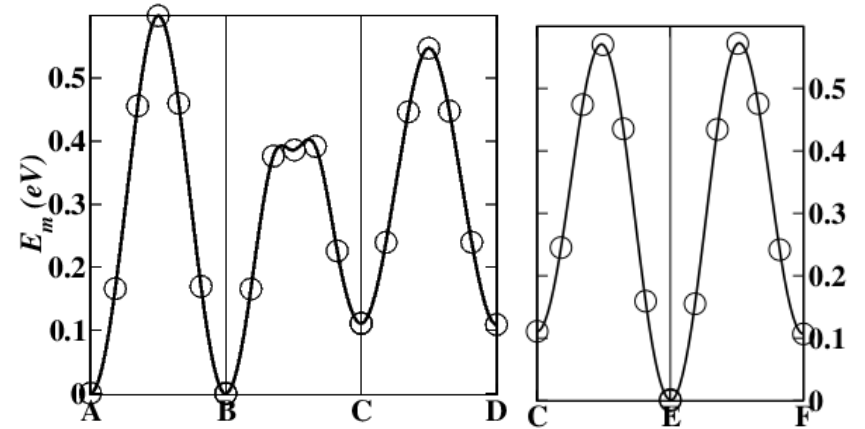
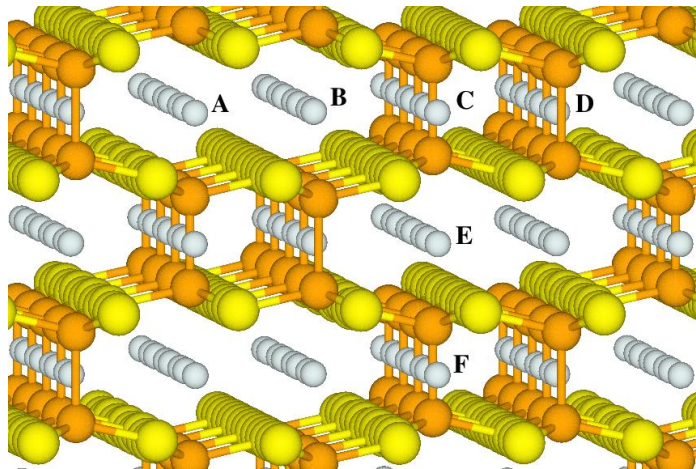
$2.38 \times 10^{-7} \text{ S/cm}$ at 25°C and $2.33 \times 10^{-6} \text{ S/cm}$ at 100°C
 $\text{Li}_4\text{P}_2\text{S}_6$ pressed pellets with blocking (Al/C) electrodes

Li/ $\text{Li}_4\text{P}_2\text{S}_6$ /Li cells could not be cycled

Simulations of ion mobility using Nudged Elastic Band Model

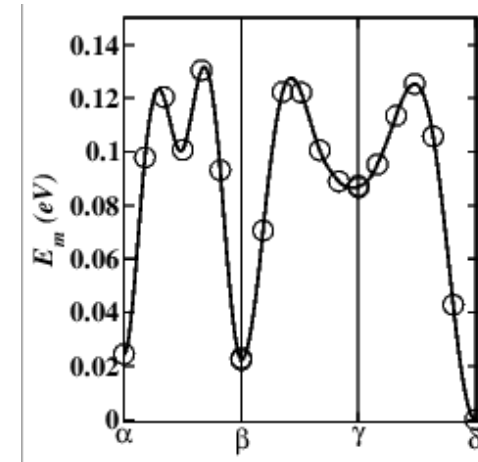
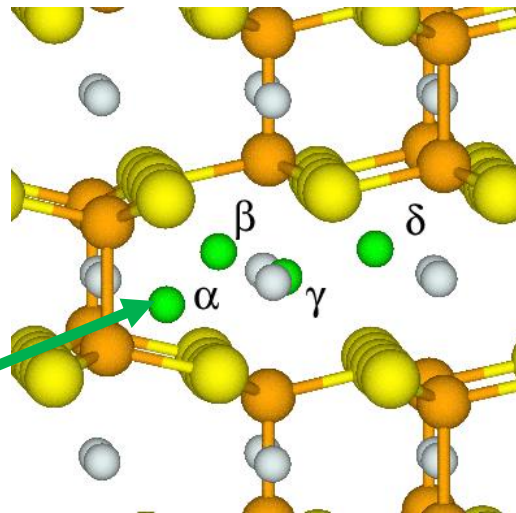
Vacancy mechanism:
 $\Delta E > 0.6 \text{ eV}$

- Li 
- P 
- S 

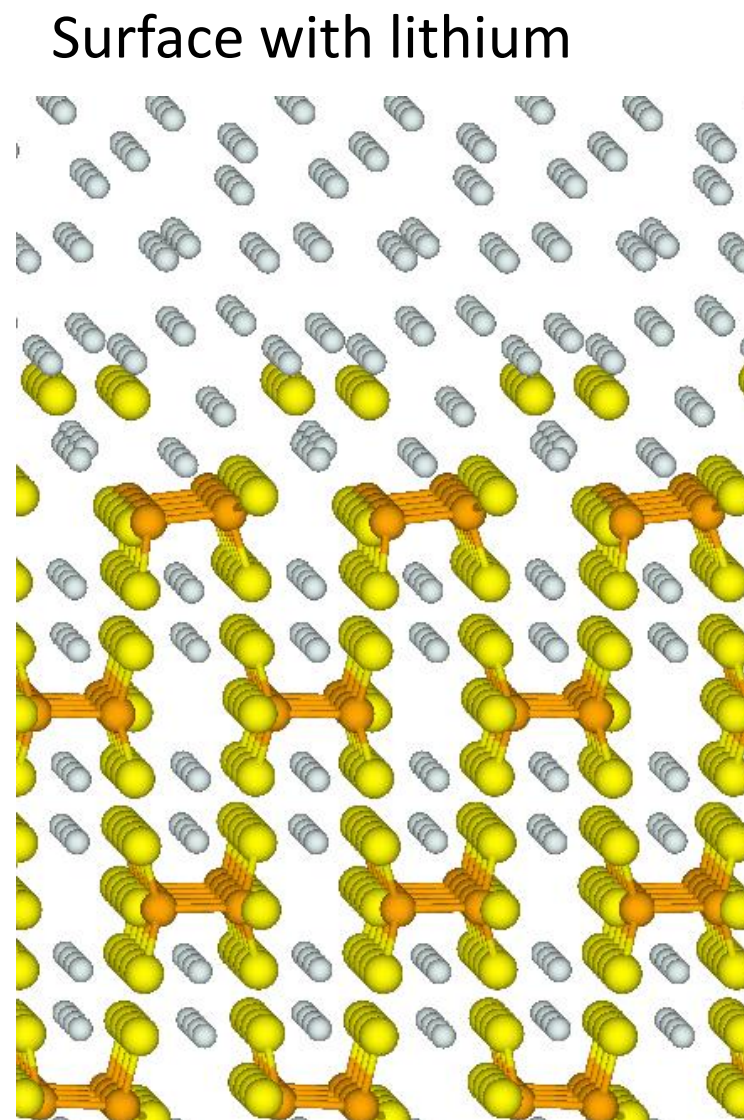
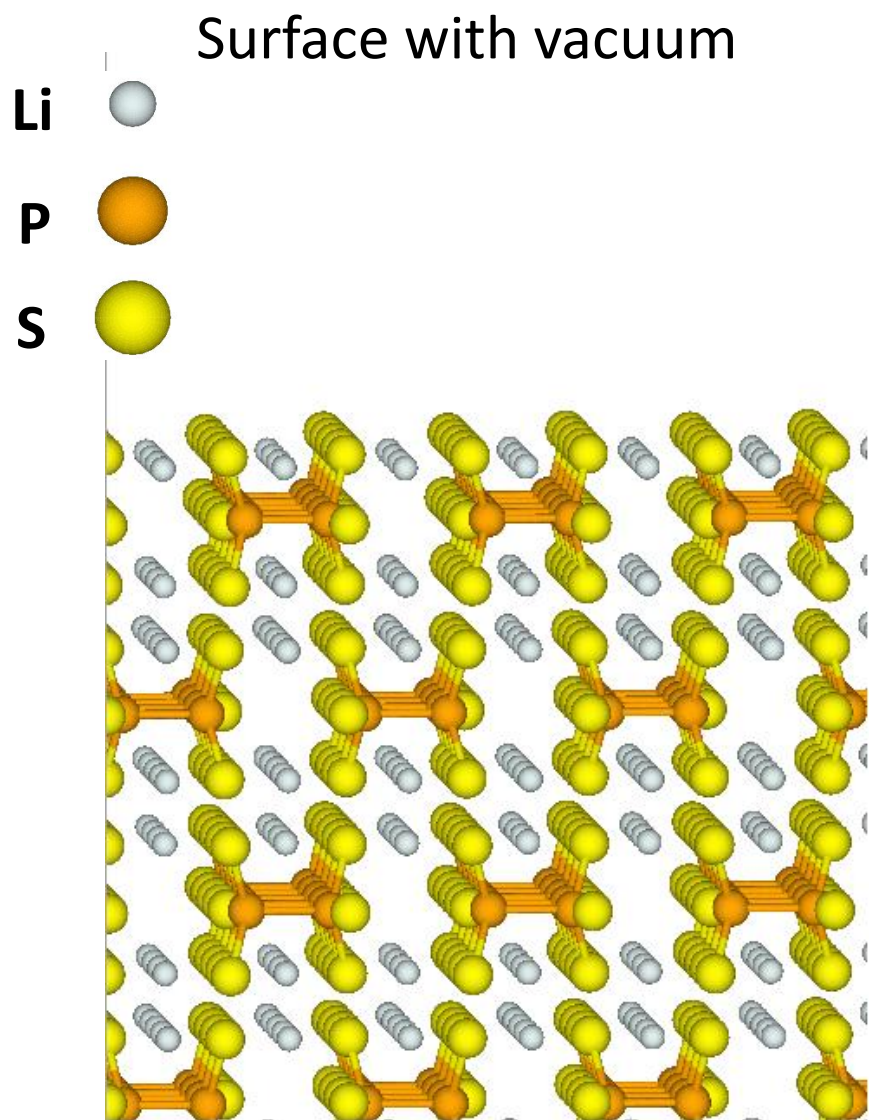


Interstitial mechanism:
 $\Delta E > 0.1 \text{ eV}$

Possible interstitial sites



Models of $\text{Li}_4\text{P}_2\text{S}_6/\text{Li}$ interfaces -- Surface parallel to P-P bonds:

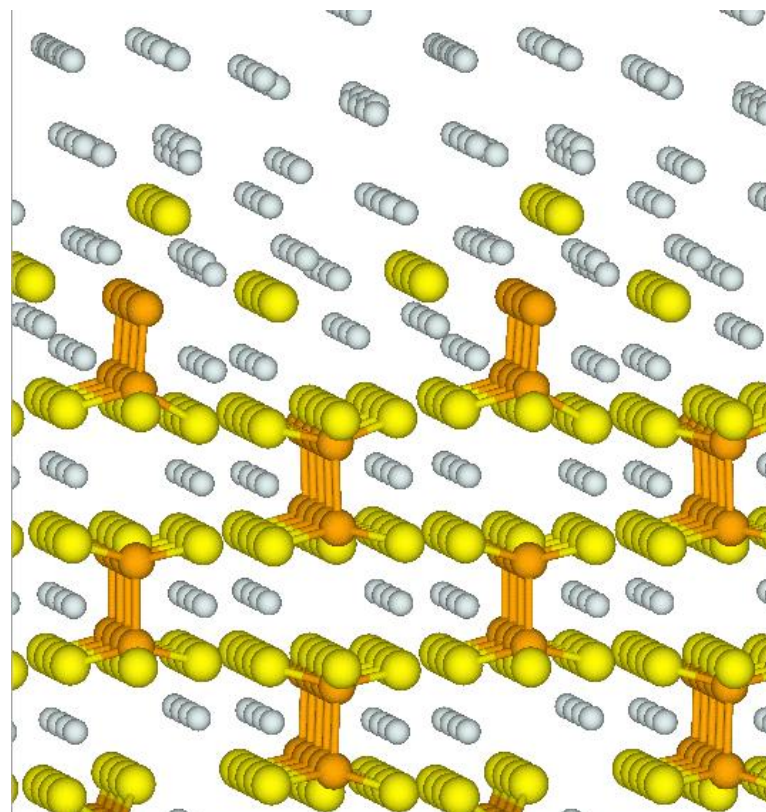
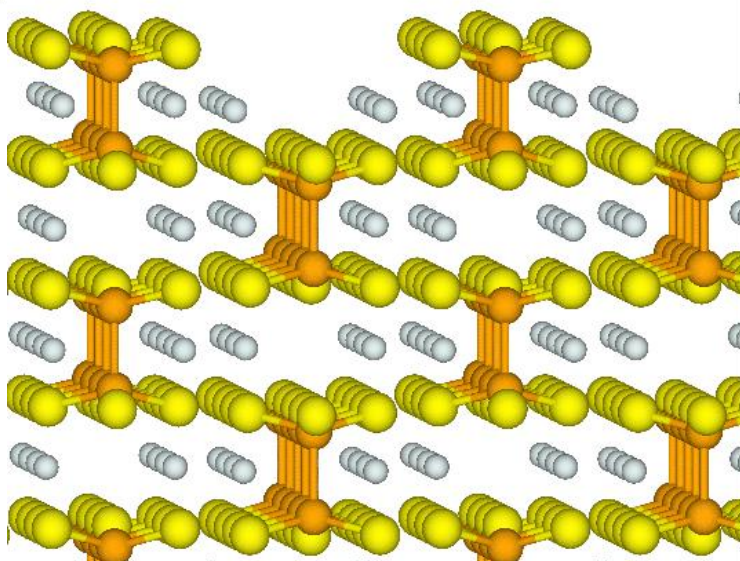
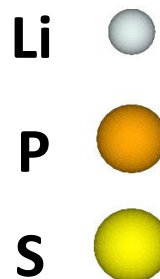


Models of $\text{Li}_4\text{P}_2\text{S}_6/\text{Li}$ interfaces --

Surface with vacuum

Surface perpendicular to P-P bonds:

Surface with lithium



Reactivity of $\text{Li}/\text{Li}_4\text{P}_2\text{S}_6$ interface models
consistent with experimental observation that
 $\text{Li}/\text{Li}_4\text{P}_2\text{S}_6/\text{Li}$ cells could not be cycled

10/14/2015

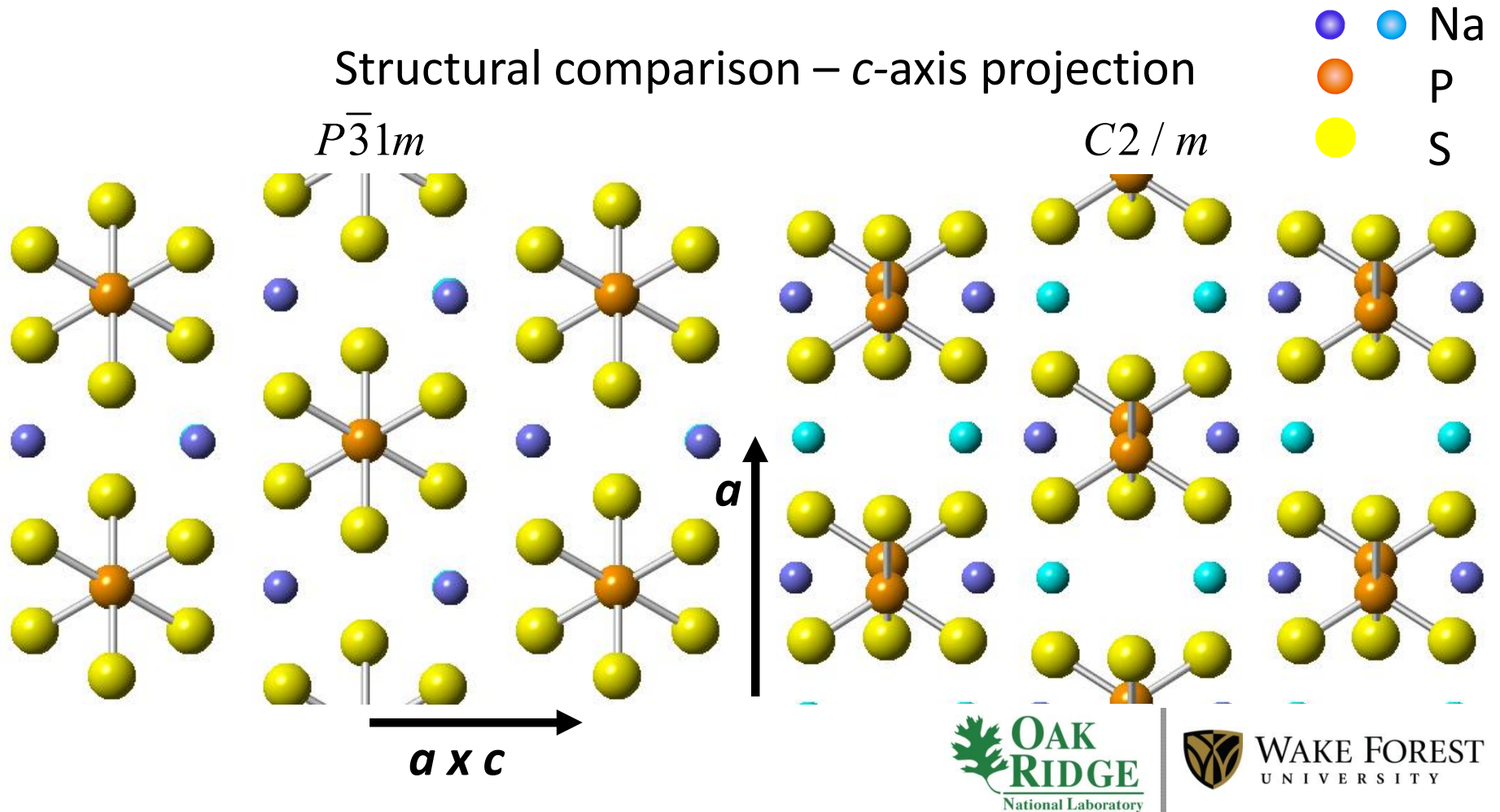
228th ECS Meeting

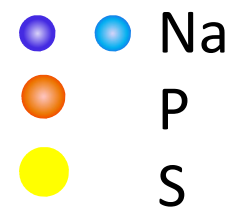


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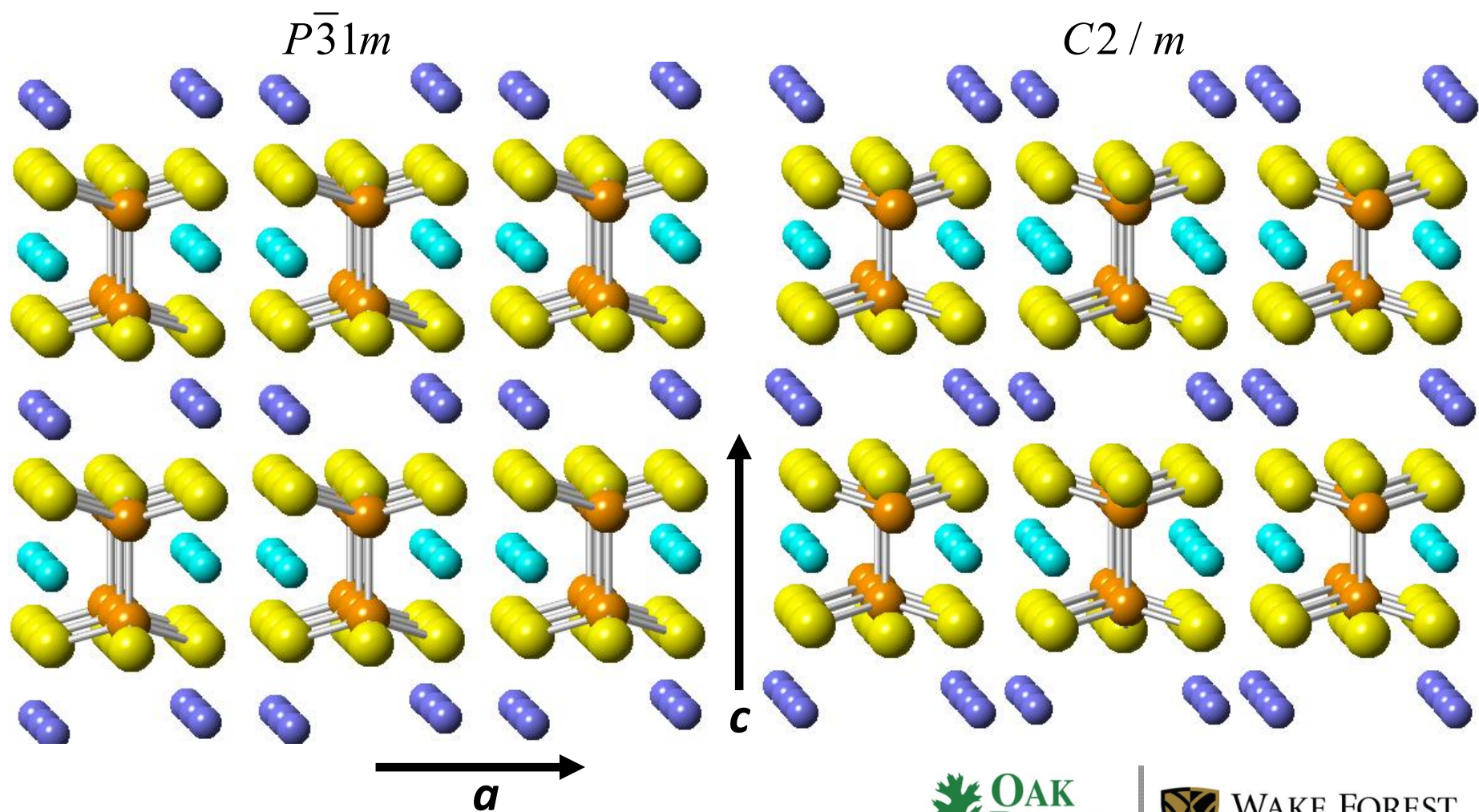
Preliminary results for $\text{Na}_4\text{P}_2\text{S}_6$:

Kuhn et al., ZAAC **640**, 689-692 (2014) synthesized single crystals with a monoclinic structure having space group $C2/m$ with similarities to the trigonal structure with $P\bar{3}1m$ space group





Structural comparison – view including c-axis



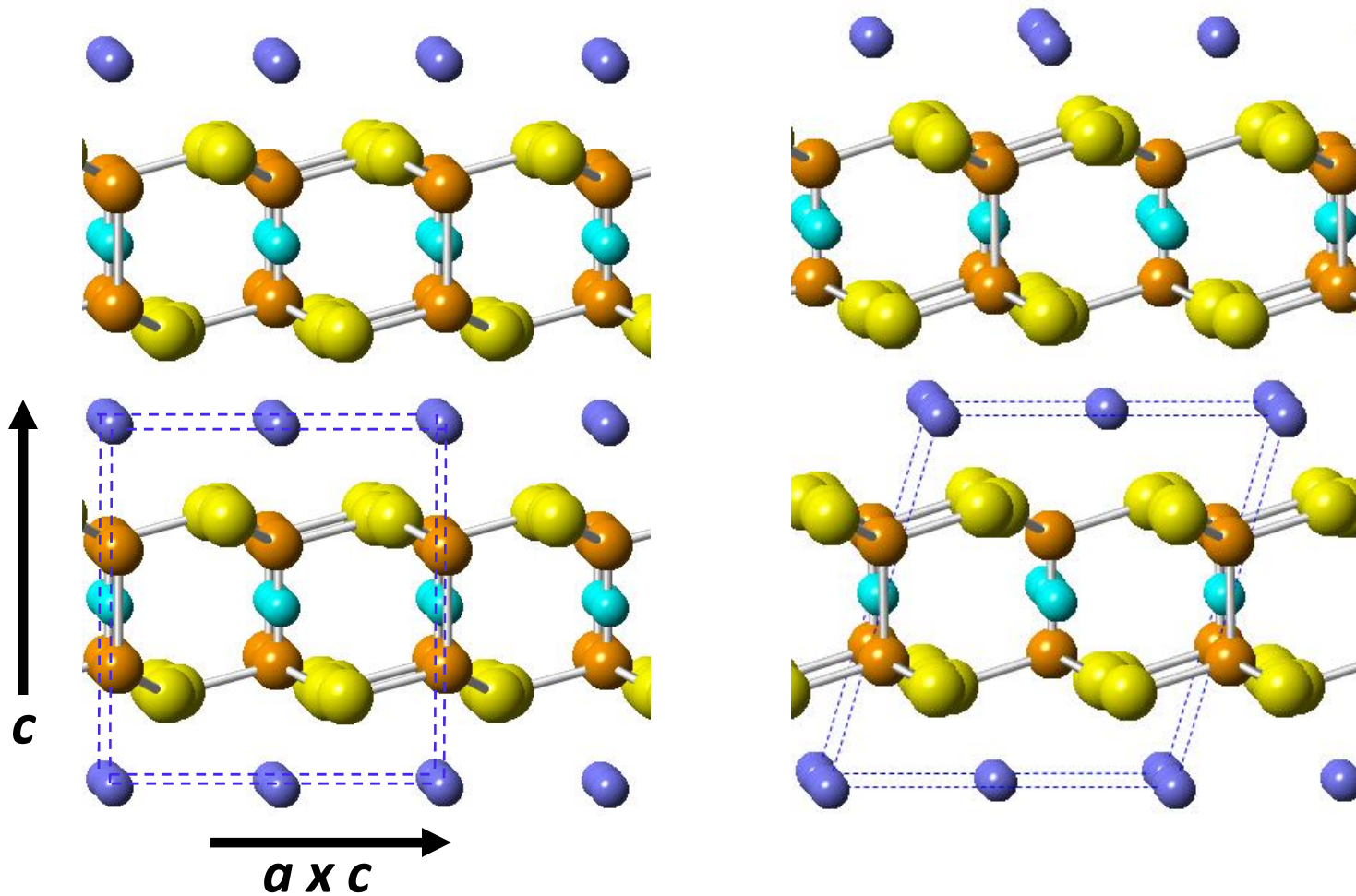


Structural comparison – view including c-axis

- Na
- P
- S

$P\bar{3}1m$

$C2/m$



Preliminary results for $\text{Na}_4\text{P}_2\text{S}_6$:

Calculated heats of formation (eV per formula unit) for $\text{Na}_4\text{P}_2\text{S}_6$ and $\text{Li}_4\text{P}_2\text{S}_6$ in 4 structural models

	$\text{Na}_4\text{P}_2\text{S}_6$	$\text{Li}_4\text{P}_2\text{S}_6$
Kuhn structure	-11.47 eV	-12.07 eV
Structure "b"	-11.47 eV	-12.42 eV
Structure "c"	-11.56 eV	-12.46 eV
Structure "d"	-11.56 eV	-12.46 eV

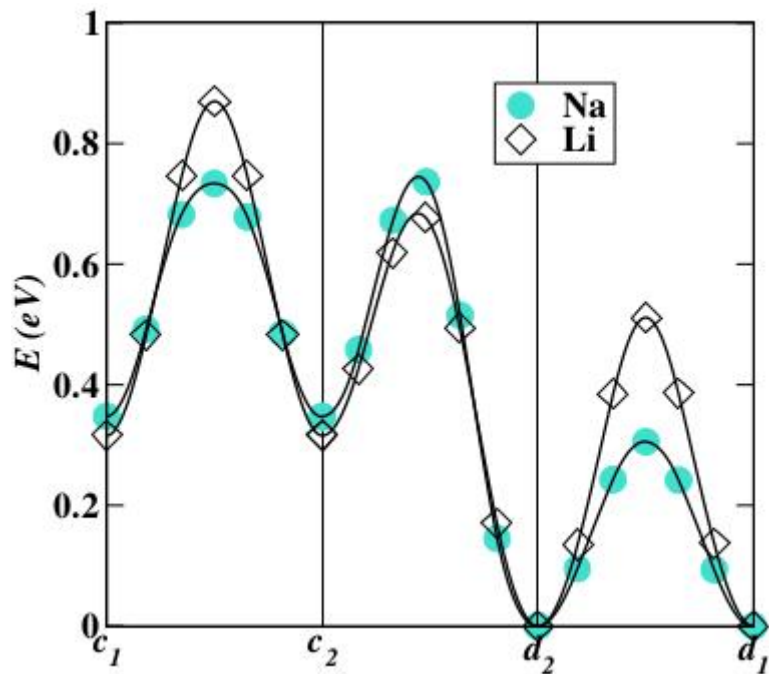
} Models of disordered Mercier structure

→ Calculations find the most stable structure for both $\text{Na}_4\text{P}_2\text{S}_6$ and $\text{Li}_4\text{P}_2\text{S}_6$ to be the disordered Mercier structure, suggesting that the Kuhn structure is meta-stable.

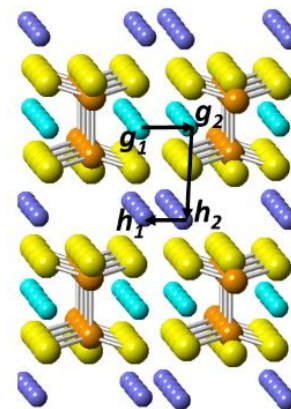
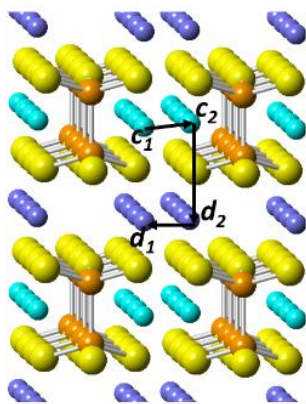
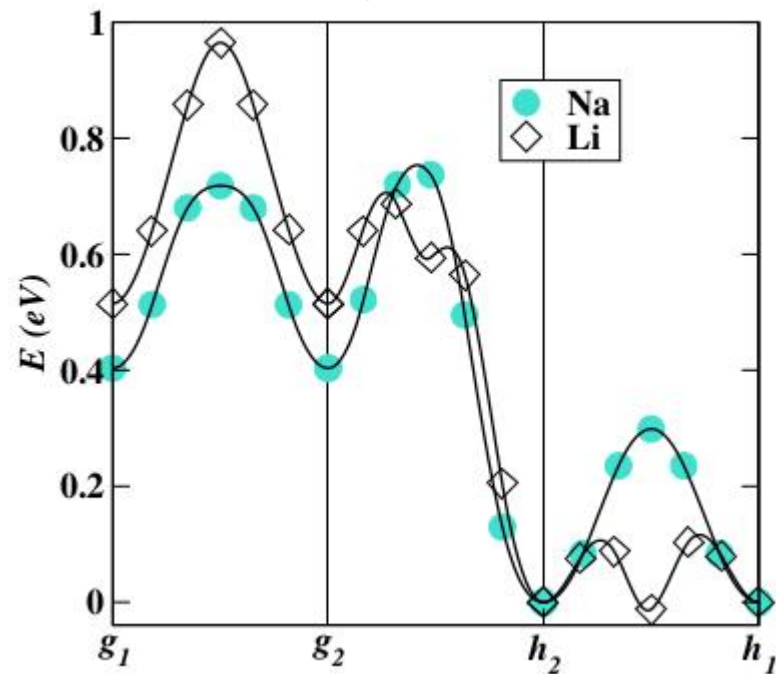
Na₄P₂S₆

Comparison of vacancy migration of Na₄P₂S₆ and Li₄P₂S₆

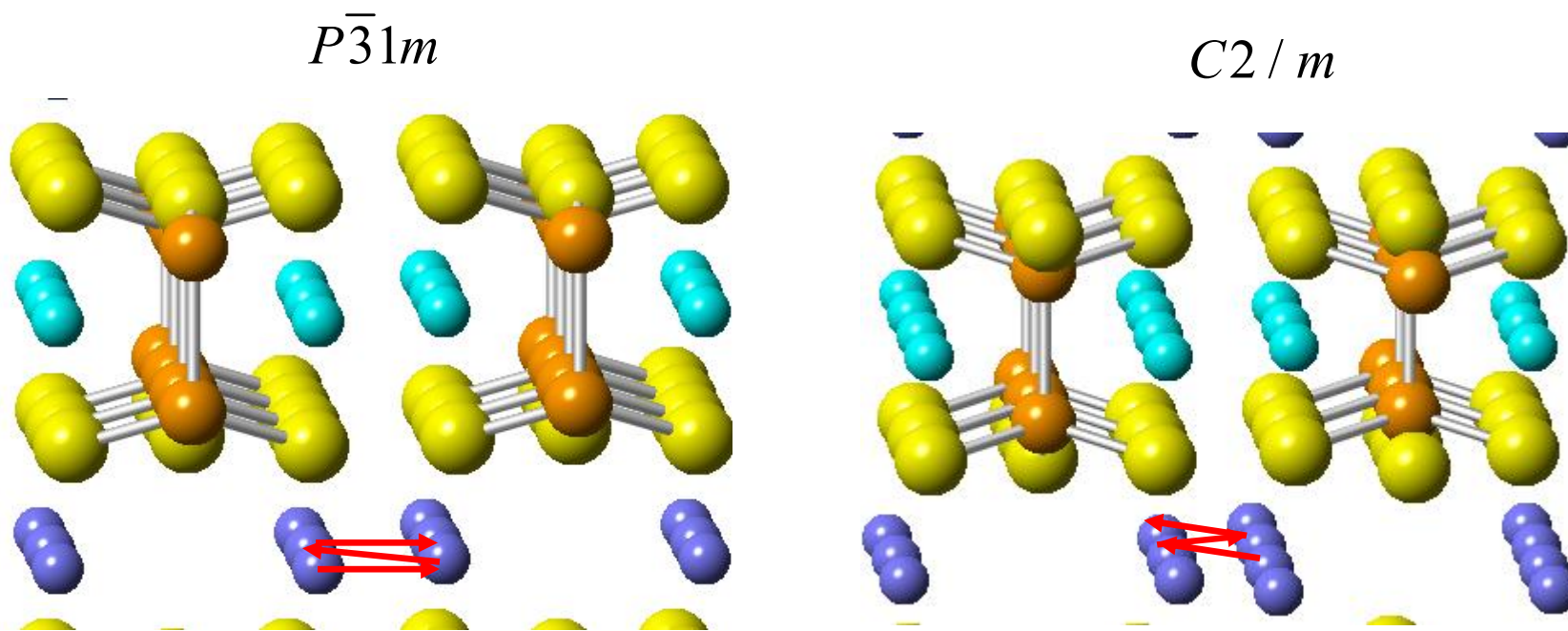
$P\bar{3}1m$



$C2/m$



- ● Na
- P
- S



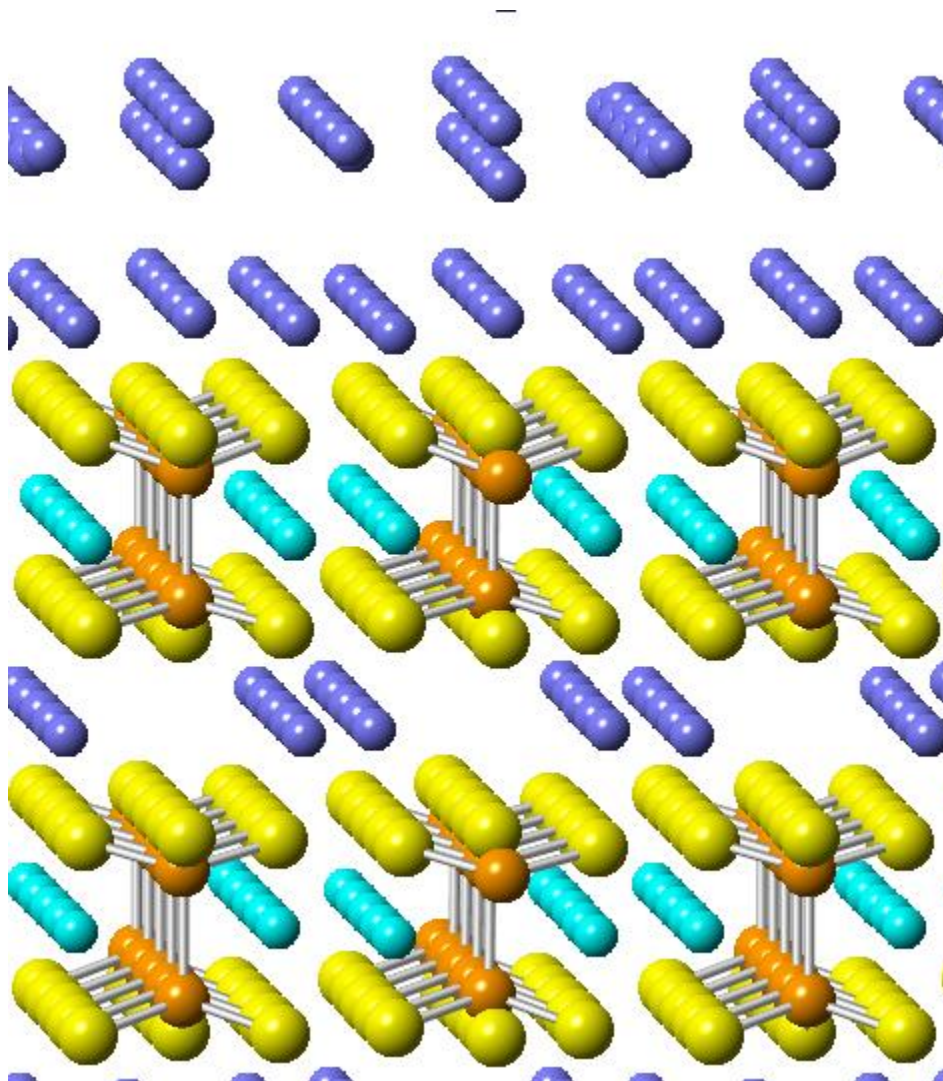
- ● Na
- P
- S

Minimum ion vacancy migration energies

	$P\bar{3}1m$	$C2/m$
$\text{Na}_4\text{P}_2\text{S}_6$	0.3 eV	0.3 eV
$\text{Li}_4\text{P}_2\text{S}_6$	0.5 eV	0.1 eV

Model of $\text{Na}_4\text{P}_2\text{S}_6/\text{Na}$ interface in Kuhn structure

- ● Na
- P
- S



meta-stable
ideal interface

Conclusions:

- $\text{Li}_4\text{P}_2\text{S}_6$ and $\text{Na}_4\text{P}_2\text{S}_6$ have interesting structural properties; simulations find the most stable structure for both to be the disordered Mercier structure, suggesting that the Kuhn structure is meta-stable.
- Experimental structural studies for $\text{Li}_4\text{P}_2\text{S}_6$ agree with the simulations; material is found to be remarkably temperature independent and thermally stable relative to other thio-phosphates.
- Measurements find $\text{Li}_4\text{P}_2\text{S}_6$ to have low ionic conductivity; simulations suggest that $\text{Na}_4\text{P}_2\text{S}_6$ may have more favorable ionic conductivity.
- Models of ideal $\text{Li}_4\text{P}_2\text{S}_6/\text{Li}$ interfaces find broken P—S bonds; $\text{Na}_4\text{P}_2\text{S}_6/\text{Na}$ interfaces in the Kuhn structure may be slightly more stable