## PHY 711 – Problem Set # 9

Continue reading Chapter 3 in Fetter and Walecka.

Consider the following Lagrangians. For each, determine the equations and constants of motion. Also write the corresponding Hamiltonian. Assume that  $A,\,B,\,M,\,g,\,h,\,q,$  and c are constant parameters.

1.

$$L(\theta, \phi, \psi, \dot{\theta}, \dot{\phi}, \dot{\psi}) = \frac{1}{2} A \left( \dot{\phi}^2 \sin^2(\theta) + \dot{\theta}^2 \right) + \frac{1}{2} B \left( \dot{\phi} \cos(\theta) + \dot{\psi} \right)^2 - Mgh \cos(\theta).$$

2.

$$L(x, y, z, \dot{x}, \dot{y}, \dot{z}) = \frac{1}{2}M(\dot{x}^2 + \dot{y}^2 + \dot{z}^2) + \frac{1}{2}\frac{q}{c}B(x\dot{y} - y\dot{x}).$$