

Physics 712 Chapter 7 Solutions

1. In Richard Williams' lab, a laser can (briefly) produce 50 GW of power and be focused on a region of size $1 \mu\text{m}^2$. How large are the maximum electric and magnetic fields?
2. Suppose a perfect polarizer extracts from a pure wave in the z -direction just the polarization $\epsilon_x = \hat{x}$, $\epsilon_y = \hat{y}$, $\epsilon_l = \frac{1}{\sqrt{2}}(\hat{x} + \hat{y})$, or $\epsilon_r = \frac{1}{\sqrt{2}}(\hat{x} - \hat{y})$. In each case, write the resulting intensity in terms of just the Stokes parameters. Find a relationship between the four intensities I_x, I_y, I_l, I_r .
3. Some materials are *birefringent*: they have different indices of refraction in two directions. Suppose a material has index of refraction n_x for electric fields in the x -direction and index of refraction n_y in the y -direction, with $n_y > n_x$. Now imagine a wave going through such a region of thickness d which has initial polarization $\epsilon = \frac{1}{\sqrt{2}}(\hat{x} + \hat{y})$. Show there is a minimum distance d such that the wave will now be circularly polarized. A device with this thickness is called a *quarter wave plate*. Then tell me what happens if the same initial wave were passed through two, three, or four quarter-wave plates. What would happen if the same initial wave were put through two, three, or four quarter-wave plates?
4. A plane wave starts in a region with index of refraction n and then is normally incident on a region with index n' of thickness d , after which it then exits to a region of index n . For what thicknesses d will there be *no* reflected wave? Will the same thickness d work for all frequencies? Explain why soap bubbles often look colorful in reflected light.

